

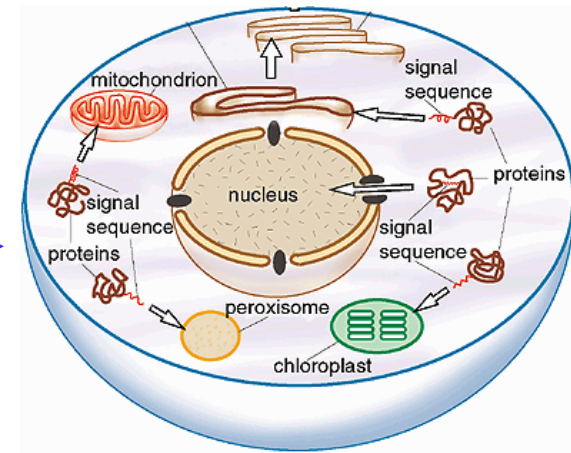
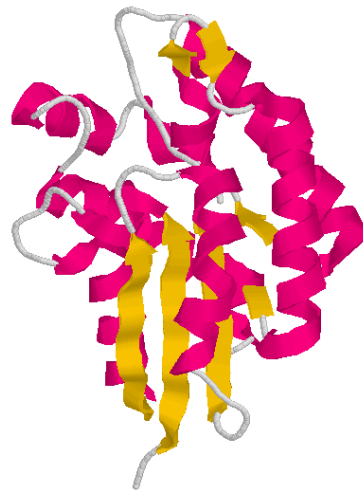
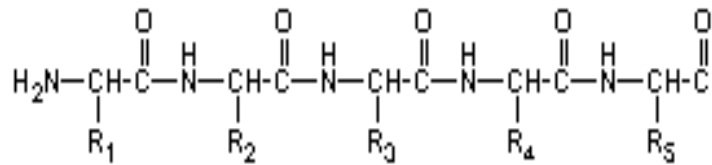
Template Based Protein Structure Modeling

Jianlin Cheng, PhD

Professor
Department of EECS
Informatics Institute
University of Missouri, Columbia
2019

Sequence, Structure and Function

AGCWY.....

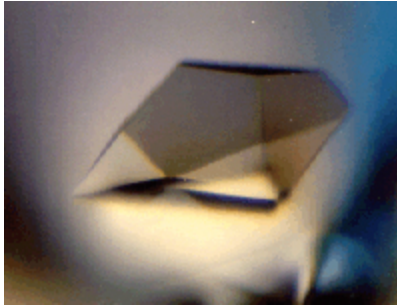


Cell

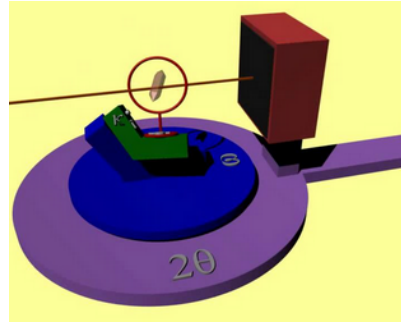
Protein Structure Determination

- X-ray crystallography
- Nuclear Magnetic Resonance (NMR) Spectroscopy
- Cryo-Electron Microscopy
- X-ray: any size, accurate (1-3 Angstrom (10^{-10} m)), sometime hard to grow crystal
- NMR: small to medium size, moderate accuracy, structure in solution

X-Ray Crystallography



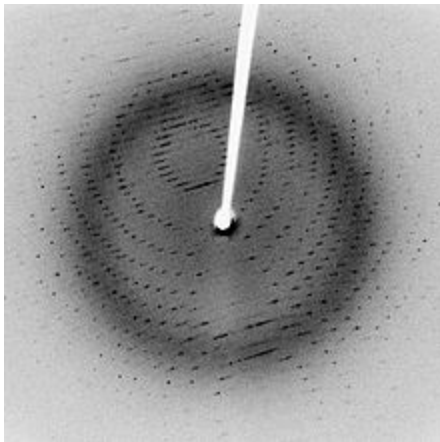
A protein crystal



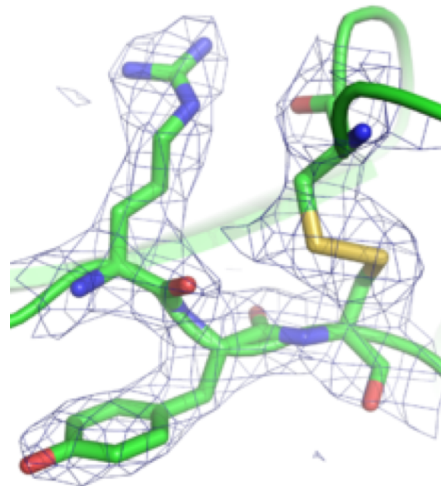
Mount a crystal



Diffractometer



Diffraction



Protein structure



Kendrew and Perutz won 1962
Nobel Prize



[Pacific Northwest National Laboratory](#)'s high magnetic field (800 MHz, 18.8 T) NMR spectrometer being loaded with a sample.

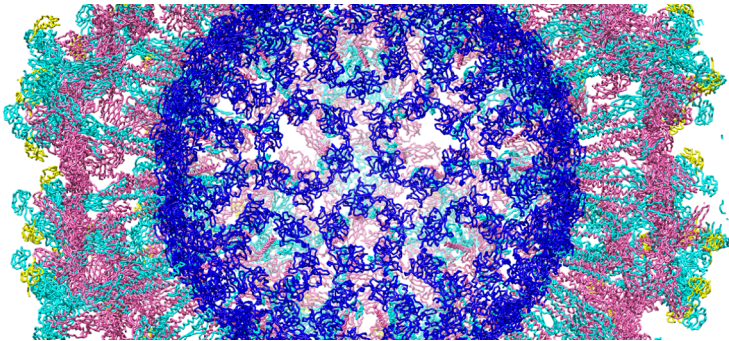
[Wikipedia, the free encyclopedia](#)

- **Key idea:** measure the distance between atoms in protein
- Build 3D structures by satisfying the distance between atoms using computational tools such as Crystallography and NMR system (CNS).



• **Kurt Wüthrich,**
Switzerland: [Nobel Prize in Chemistry 2002](#), "for his development of nuclear magnetic resonance spectroscopy for determining the three-dimensional structure of biological macromolecules in solution"

- **Cryo-EM equipment**



- Key idea: generate 2D images of proteins from different angles, and then assemble them into one 3D structure. A lot of imaging techniques used.

The Nobel Prize in Chemistry 2017



© Nobel Media AB. Photo: A. Mahmoud

Jacques Dubochet

Prize share: 1/3



© Nobel Media AB. Photo: A. Mahmoud

Joachim Frank

Prize share: 1/3



© Nobel Media AB. Photo: A. Mahmoud

Richard Henderson

Prize share: 1/3

Storage in Protein Data Bank

RCSB PDB An Information Portal to 115306 Biological Macromolecular Structures
PROTEIN DATA BANK

Search by PDB ID, author, macromolecule, sequence, or ligands

Advanced Search | Browse by Annotations | Search History (1) | Previous Results (12578)

Logos: PDB-101, Worldwide Protein Data Bank, EMDatabank, Nucleic Acid Database, Structural Biology Knowledgebase

Structure Summary | 3D View | Annotations | Sequence | Sequence Similarity | Structure Similarity | Experiment

Biological Assembly 1

4KVP

Human p53 Core Domain Mutant V157F
DOI: 10.2210/pdb4kvp/pdb Entry 4KVP **supersedes** 2QXA

Classification: **APOPTOSIS**
Deposited: 2013-05-22 Released: 2013-07-31
Deposition author(s): [Wallentine, B.D.](#), [Wang, Y.](#), [Luecke, H.](#)
Organism: [Homo sapiens](#)
Expression System: Escherichia coli
Mutation(s): 1

Structural Biology Knowledgebase: 4KVP (2 models >14 annotations) [SBKB.org](#)

Experimental Data Snapshot

Method: X-RAY DIFFRACTION
Resolution: 1.5 Å
R-Value Free: 0.210
R-Value Work: 0.174

wwPDB Validation

| Metric | Percentile Ranks | Value |
|-----------------------|------------------|-------|
| Rfree | | 0.228 |
| Clashscore | | 5 |
| Ramachandran outliers | | 0 |
| Sidechain outliers | | 1.3% |
| RSRZ outliers | | 1.0% |

Worse | Better
■ Percentile relative to all X-ray structures
□ Percentile relative to X-ray structures of similar resolution

Literature

View in 3D: [JSmol](#) or [PV](#) (in Browser)

Standalone Viewers
[Simple Viewer](#) [Protein Workshop](#)
[Ligand Explorer](#) [Kiosk Viewer](#)

Protein Symmetry: Asymmetric (View in 3D)
Protein Stoichiometry: Monomer

Search database

Search Demo: Human P53 protein – 1KVP

<http://www.rcsb.org/pdb/explore/explore.do?structureId=4KVP>

PDB Format (2C8Q, insulin)

```
HEADER      HORMONE                                06-DEC-05   2C8Q
TITLE       INSULINE(1SEC) AND UV LASER EXCITED FLUORESCENCE
COMPND      MOL_ID: 1;
COMPND      2 MOLECULE: INSULIN A CHAIN;
COMPND      3 CHAIN: A;
COMPND      4 MOL_ID: 2;
COMPND      5 MOLECULE: INSULIN B CHAIN;
COMPND      6 CHAIN: B
SOURCE      MOL_ID: 1;
SOURCE      2 ORGANISM_SCIENTIFIC: HOMO SAPIENS;
SOURCE      3 ORGANISM_COMMON: HUMAN;
SOURCE      4 ORGAN: PANCREAS;
SOURCE      5 MOL_ID: 2;
SOURCE      6 ORGANISM_SCIENTIFIC: HOMO SAPIENS;
SOURCE      7 ORGANISM_COMMON: HUMAN;
SOURCE      8 ORGAN: PANCREAS
KEYWDS      LASER, UV, CARBOHYDRATE METABOLISM, HORMONE, DIABETES
KEYWDS      2 MELLITUS, GLUCOSE METABOLISM
EXPDTA      X-RAY DIFFRACTION
AUTHOR      X.VERNEDE,B.LAVault,J.OHANA,D.NURIZZO,J.JOLY,L.JACQUAMET,
AUTHOR      2 F.FELISAZ,F.CIPRIANI,D.BOURGEOIS
REVDATE     1 08-MAR-06 2C8Q 0
JRNL        AUTH X.VERNEDE,B.LAVault,J.OHANA,D.NURIZZO,J.JOLY,
JRNL        AUTH 2 L.JACQUAMET,F.FELISAZ,F.CIPRIANI,D.BOURGEOIS
JRNL        TITL UV LASER-EXCITED FLUORESCENCE AS A TOOL FOR THE
JRNL        TITL 2 VISUALIZATION OF PROTEIN CRYSTALS MOUNTED IN
JRNL        TITL 3 LOOPS.
JRNL        REF ACTA CRYSTALLOGR.,SECT.D V. 62 253 2006
JRNL        REFN ASTM ABCRE6 DK ISSN 0907-4449
REMARK      2
REMARK      2 RESOLUTION. 1.95 ANGSTROMS.
REMARK      3
REMARK      3 REFINEMENT.
REMARK      3 PROGRAM : REFMAC 5.2.0005
REMARK      3 AUTHORS : MURSHUDOV,VAGIN,DODSON
REMARK      3
REMARK      3 REFINEMENT TARGET : MAXIMUM LIKELIHOOD
```


Structure Visualization

- Rasmol
(<http://www.umass.edu/microbio/rasmol/getras.htm>)
- MDL Chime (plug-in)
(<http://www.mdl.com/products/framework/chime/>)
- **Jmol:** <http://jmol.sourceforge.net/>
- **JSMol:** java script version
- **Pymol:** <http://pymol.sourceforge.net/>
- **Chimera:** <https://www.cgl.ucsf.edu/chimera/>

JSMol (4KVP, Human P53)

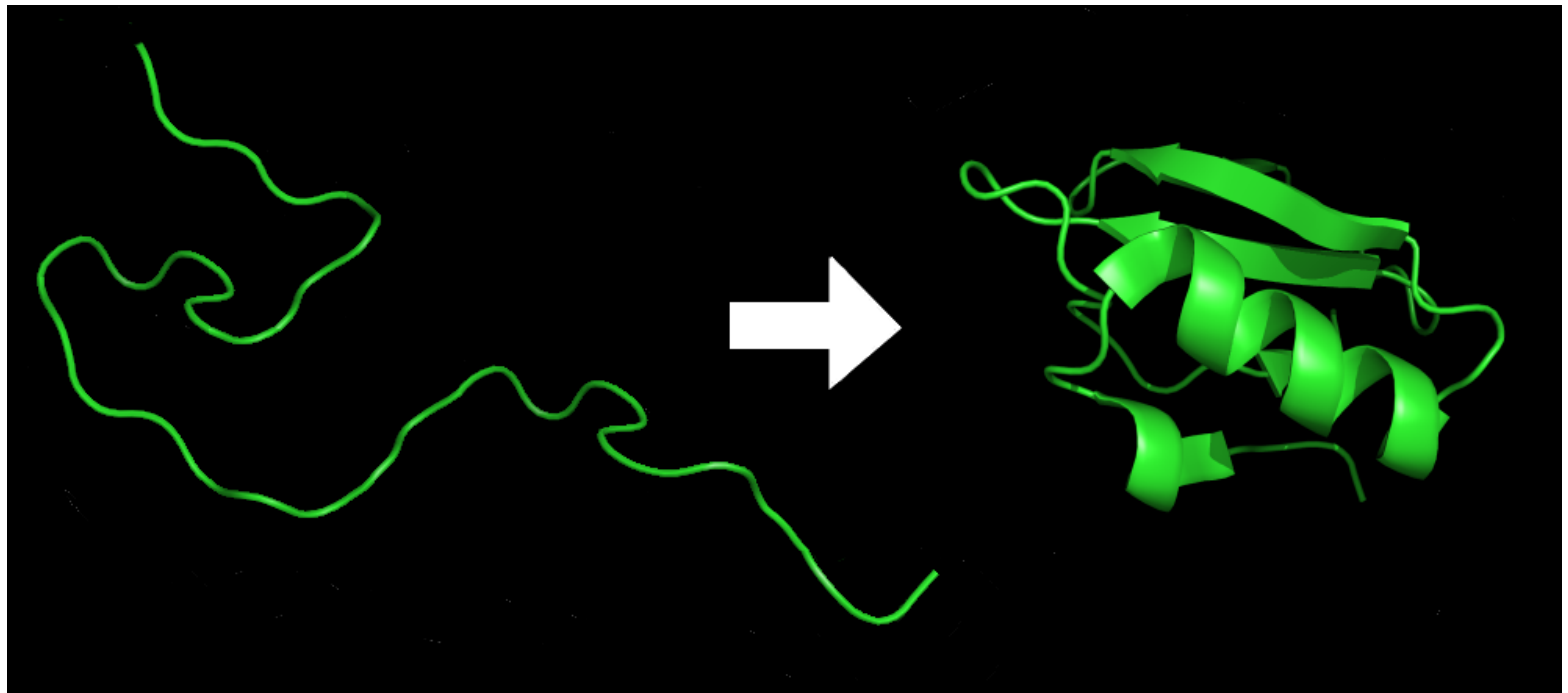
- JSMol:

<http://www.rcsb.org/pdb/explore/jmol.do?structureId=4KVP&bionumber=1>

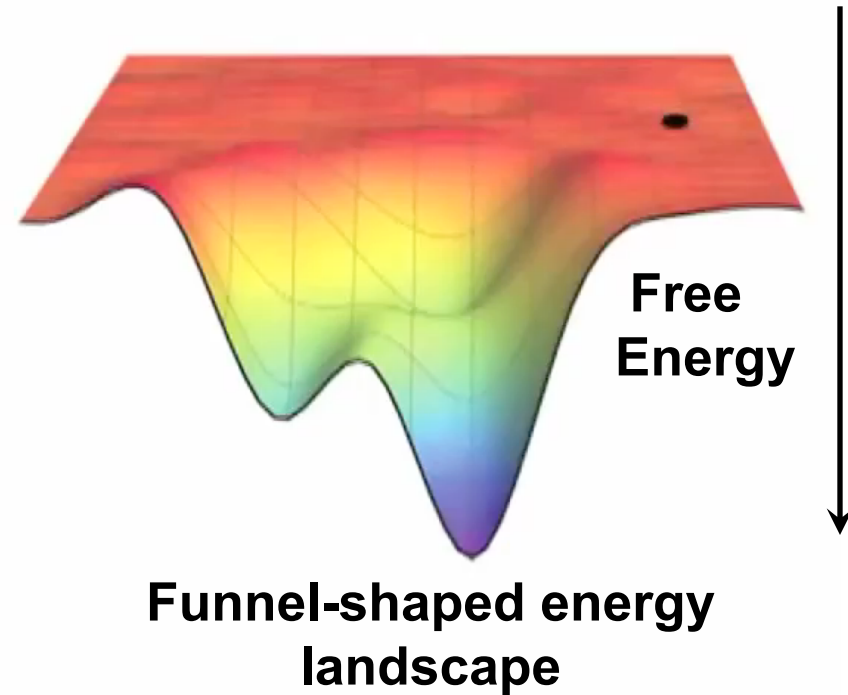
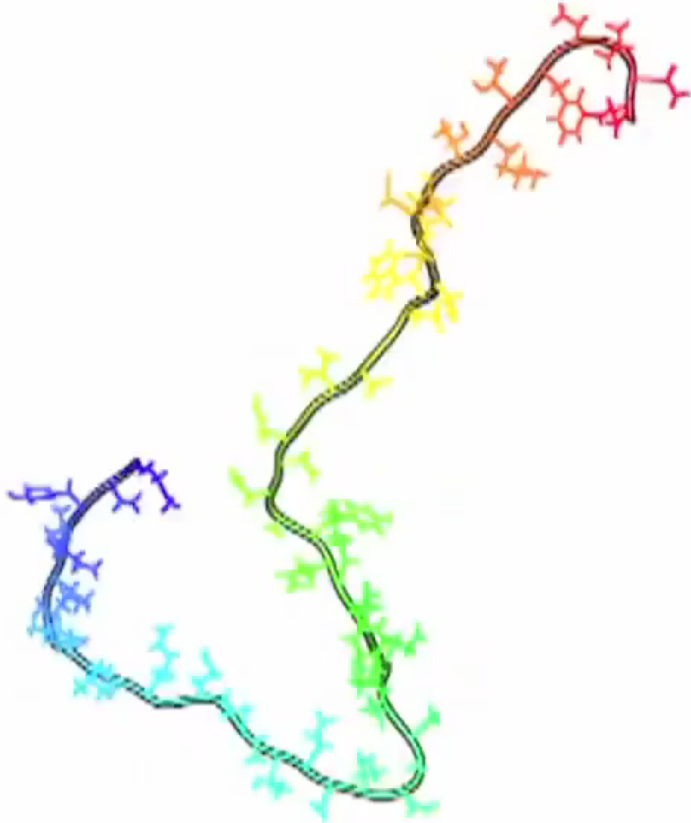
- JMOL: 1VJP
- Identify residues
- Recognize atoms
- Recognize peptide bonds
- Identify backbone
- Identify side chain
- Analyze different visualization style

Protein Folding

<http://www.youtube.com/watch?v=fvBO3TqJ6FE&feature=fvw>



Computational Protein Folding by MULTICOM (Demo)

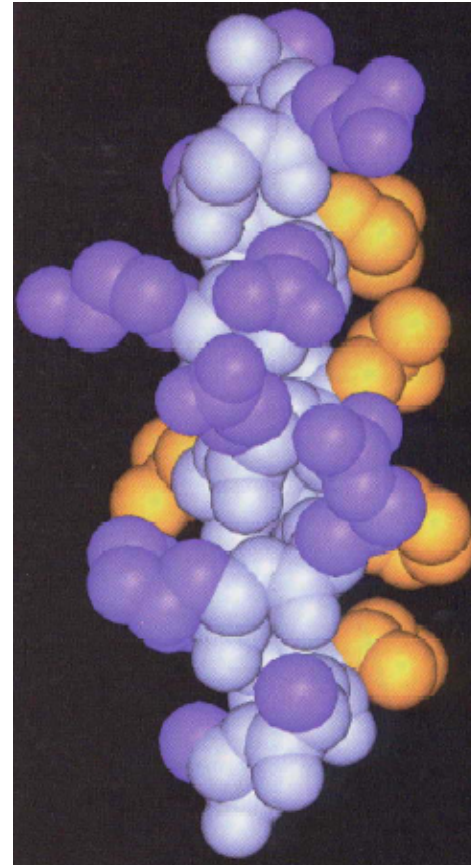
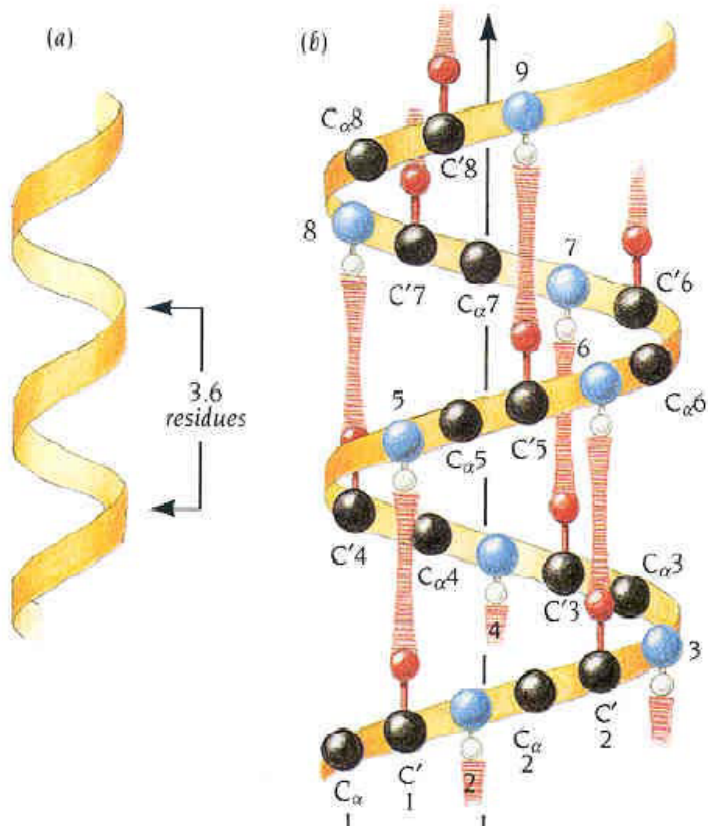


AlphaFold Movie

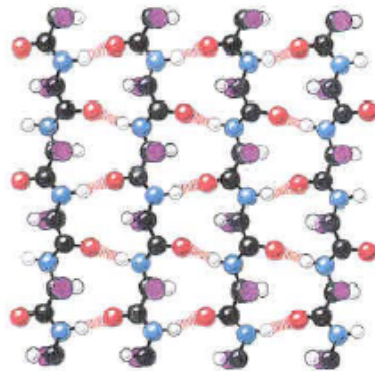
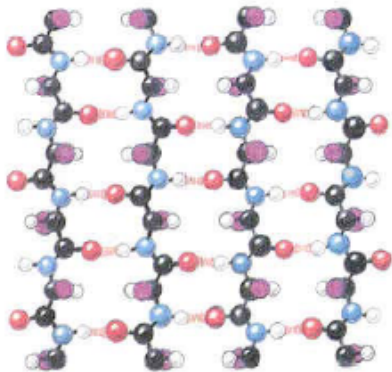
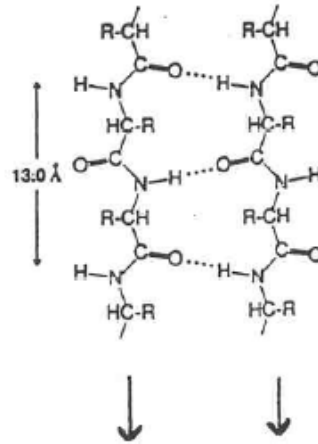
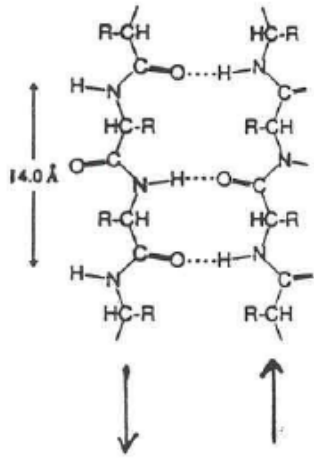
- <https://deepmind.com/blog/alphafold/#gif-242>



Alpha-Helix

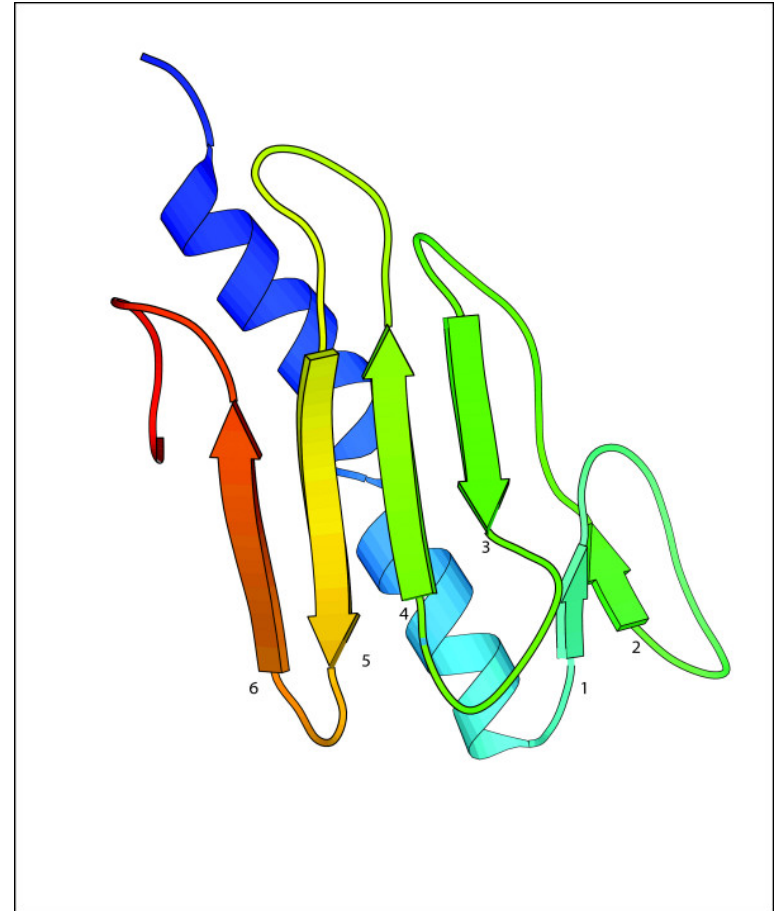


Beta-Sheet

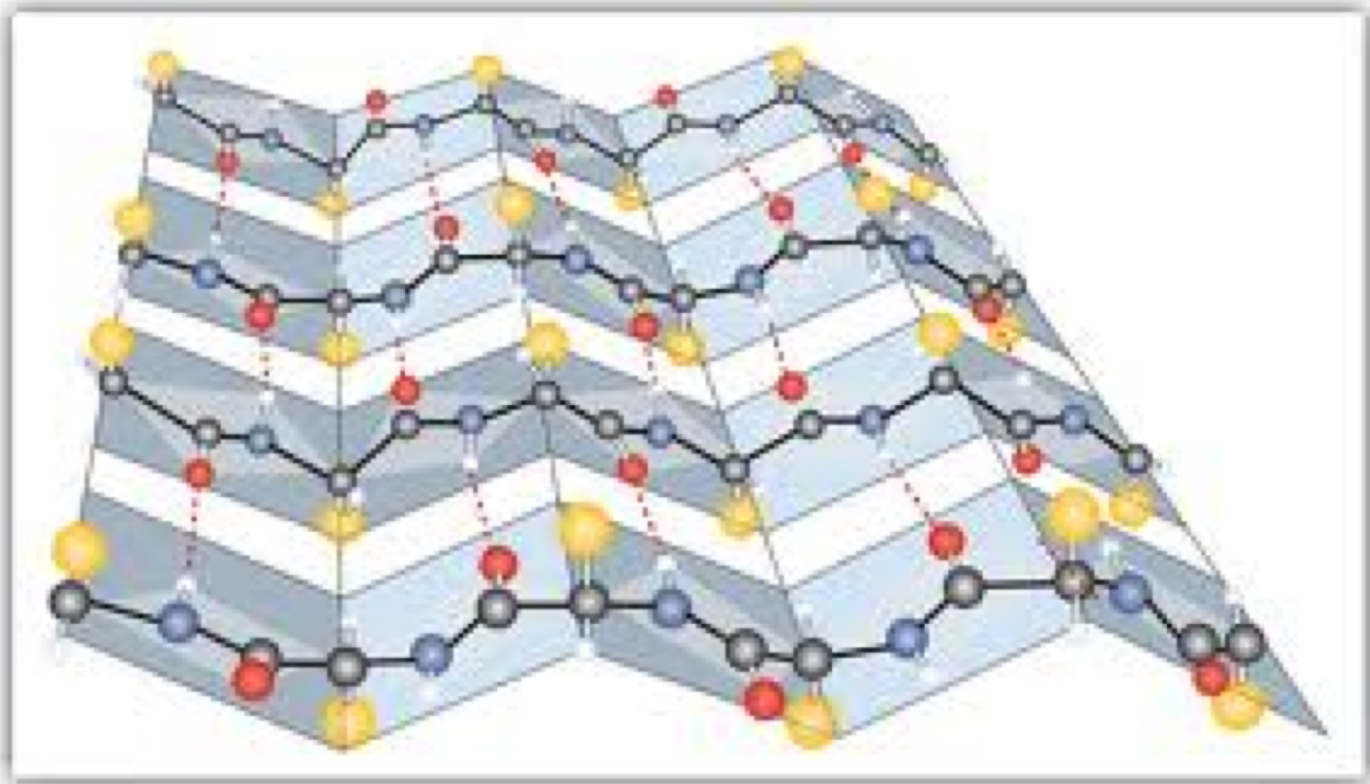


Anti-Parallel

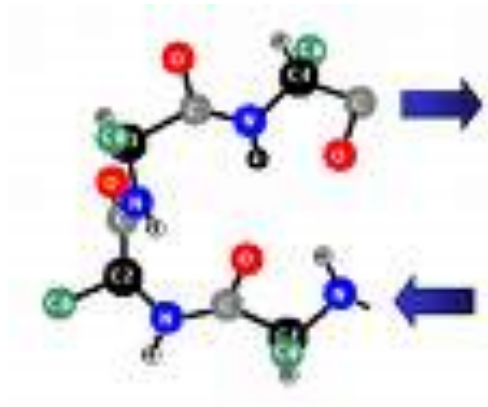
Parallel



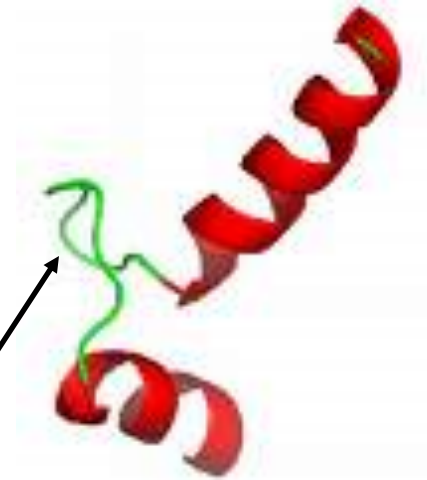
Beta-Sheet



Non-Repetitive Secondary Structure



Beta-Turn



Loop

Announcement – Next Class

Data-driven modeling of protein structure, 3D genome and gene regulatory network

Jianin Cheng

**Hosted by:
Dr. Zezong Gu**

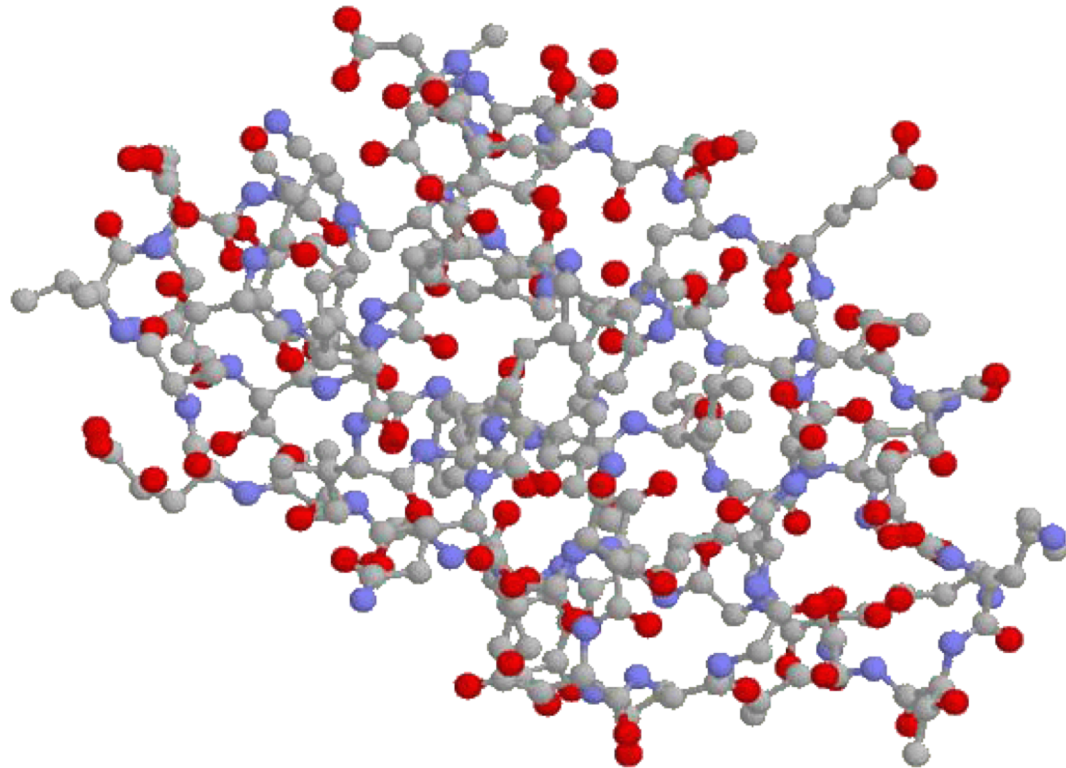
**Monday, February, 11, 2019
4:00 p.m.**

**Pathology Conference Room
MA223 Medical Sciences Building Annex**

Refreshments provided at 3:50 pm

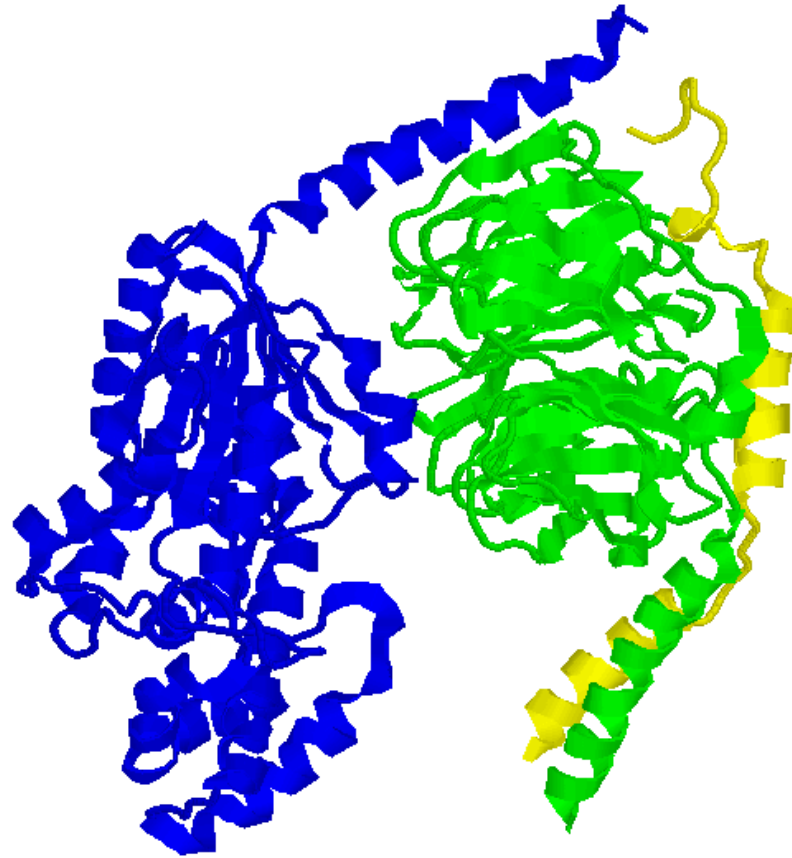


myoglobin



tertiary structure
(all atom)

Quaternary Structure: Complex



G-Protein Complex

Structure Analysis

- Assign secondary structure for amino acids from 3D structure
- Generate solvent accessible area for amino acids from 3D structure
- Most widely used tool: DSSP (Dictionary of Protein Secondary Structure: Pattern Recognition of Hydrogen-Bonded and Geometrical Features. **Kabsch and Sander, 1983**)

DSSP server: <http://bioweb.pasteur.fr/seqanal/interfaces/dssp-simple.html>

DSSP download: <http://swift.cmbi.ru.nl/gv/dssp/>

DSSP Code:

H = alpha helix

G = 3-helix (3/10 helix)

I = 5 helix (pi helix)

B = residue in isolated beta-bridge

E = extended strand, participates in beta ladder

T = hydrogen bonded turn

S = bend

Blank = loop

DSSP Web Service

**DSSP : Definition of secondary structure of proteins given a set of 3D coordinates
(W.Kabsch, C. Sander)**

your e-mail

PDB File

or you can instead enter a PDB id.

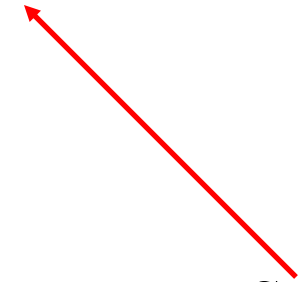
<http://bioweb.pasteur.fr/seqanal/interfaces/dssp-simple.html>

| # | RESIDUE | AA | STRUCTURE | BP1 | BP2 | ACC | N-H-->O | O-->H-N | N-H-->O | O-->H-N | TCO | KAPPA | ALPHA | PHI | PSI | X-CA | Y-CA | Z-CA | |
|----|---------|----|-----------|------|-----|-----|---------|---------|---------|----------|----------|--------|-------------------------|-------|-------|-------|------|------|------|
| 1 | 5 | A | S | | 0 | 0 | 179 | 0, 0.0 | 2,-0.0 | 0, 0.0 | 0, 0.0 | 0.000 | 360.0 | 360.0 | 360.0 | 125.7 | -8.6 | 43.0 | 43.9 |
| 2 | 6 | A | K | - | 0 | 0 | 123 | 1,-0.1 | 2,-0.4 | 37,-0.1 | 37,-0.2 | -0.235 | 360.0-108.7 | -87.0 | 151.4 | -7.5 | 41.4 | 40.6 | |
| 3 | 7 | A | T E | -a | 39 | 0A | 75 | 35,-0.6 | 37,-2.5 | 1,-0.0 | 2,-0.3 | -0.593 | 34.7-132.0 | -72.2 | 128.3 | -4.3 | 39.5 | 39.6 | |
| 4 | 8 | A | Q E | +a | 40 | 0A | 91 | -2,-0.4 | 69,-0.6 | 35,-0.2 | 2,-0.4 | -0.639 | 26.0 179.8 | -86.4 | 132.7 | -2.0 | 41.5 | 37.4 | |
| 5 | 9 | A | I E | -ab | 41 | 73A | 3 | 35,-1.9 | 37,-2.9 | -2,-0.3 | 2,-0.5 | -0.991 | 13.3-156.5-129.4 | 131.5 | -0.7 | 39.9 | 34.2 | | |
| 6 | 10 | A | R E | -ab | 42 | 74A | 48 | 67,-2.8 | 69,-1.7 | -2,-0.4 | 2,-0.4 | -0.910 | 14.8-173.2-105.2 | 126.8 | 1.6 | 41.6 | 31.8 | | |
| 7 | 11 | A | I E | -ab | 43 | 75A | 0 | 35,-2.5 | 37,-2.6 | -2,-0.5 | 2,-0.5 | -0.983 | 11.9-162.4-124.9 | 124.4 | 1.7 | 40.3 | 28.2 | | |
| 8 | 12 | A | C E | -ab | 44 | 76A | 0 | 67,-2.3 | 69,-2.6 | -2,-0.4 | 2,-0.6 | -0.931 | 6.5-159.9-100.8 | 130.8 | 3.9 | 41.2 | 25.3 | | |
| 9 | 13 | A | F E | -ab | 45 | 77A | 0 | 35,-2.2 | 37,-3.0 | -2,-0.5 | 2,-0.5 | -0.955 | 13.2-169.0-109.5 | 117.1 | 2.7 | 40.2 | 21.8 | | |
| 10 | 14 | A | V E | +ab | 46 | 78A | 0 | 67,-3.1 | 69,-2.2 | -2,-0.6 | 2,-0.3 | -0.926 | 34.8 71.1-116.5 | 129.9 | 5.6 | 40.1 | 19.4 | | |
| 11 | 15 | A | G E | S-ab | 47 | 79A | 0 | 35,-0.9 | 37,-1.9 | -2,-0.5 | 69,-0.2 | -0.921 | 70.2 -50.2 169.0-146.4 | | 5.3 | 39.9 | 15.6 | | |
| 12 | 16 | A | D S >> S- | | 0 | 0 | 4 | 67,-0.8 | 4,-2.2 | -2,-0.3 | 3,-0.6 | -0.023 | 78.2 -51.3-111.5-151.8 | | 4.2 | 41.6 | 12.4 | | |
| 13 | 17 | A | S H 3>>S+ | | 0 | 0 | 7 | 35,-0.3 | 5,-1.7 | 1,-0.2 | 4,-1.5 | 0.803 | 130.2 57.8 -67.3 -28.8 | | 1.2 | 43.5 | 11.1 | | |
| 14 | 18 | A | F H 345S+ | | 0 | 0 | 5 | 2,-0.2 | 12,-0.5 | 1,-0.2 | -1,-0.2 | 0.884 | 108.5 46.5 -68.2 -33.2 | | -1.2 | 40.8 | 12.2 | | |
| 15 | 19 | A | V H <45S+ | | 0 | 0 | 1 | -3,-0.6 | 12,-0.3 | 64,-0.2 | -2,-0.2 | 0.900 | 111.1 52.2 -68.9 -41.4 | | -0.0 | 41.1 | 15.7 | | |
| 16 | 20 | A | N H <5S- | | 0 | 0 | 71 | -4,-2.2 | -2,-0.2 | 30,-0.1 | -1,-0.2 | 0.774 | 110.8-127.0 -62.6 -26.6 | | -0.3 | 45.0 | 15.4 | | |
| 17 | 21 | A | G T ><5 - | | 0 | 0 | 5 | -4,-1.5 | 3,-2.2 | -5,-0.2 | 8,-0.4 | 0.741 | 36.4-174.6 83.1 25.3 | | -3.9 | 44.5 | 14.2 | | |
| 18 | 22 | A | T T 3 < + | | 0 | 0 | 14 | -5,-1.7 | -1,-0.2 | 1,-0.3 | -2,-0.0 | -0.199 | 68.4 29.2 -54.0 135.4 | | -3.4 | 46.6 | 11.0 | | |
| 19 | 23 | A | G T 3 S+ | | 0 | 0 | 28 | 1,-0.3 | -1,-0.3 | 159,-0.1 | 162,-0.2 | 0.121 | 86.2 120.8 94.7 -21.4 | | -6.7 | 47.0 | 9.2 | | |
| 20 | 24 | A | D X - | | 0 | 0 | 9 | -3,-2.2 | 3,-1.2 | 160,-0.2 | -1,-0.3 | -0.706 | 48.9-160.5 -79.7 117.6 | | -8.9 | 46.8 | 12.4 | | |
| 21 | 25 | A | P T 3 S+ | | 0 | 0 | 91 | 0, 0.0 | -1,-0.2 | 0, 0.0 | 159,-0.0 | 0.677 | 91.8 60.1 -70.9 -17.3 | | -10.9 | 50.1 | 12.6 | | |
| 22 | 26 | A | E T 3 S- | | 0 | 0 | 119 | -3,-0.0 | -2,-0.1 | 3,-0.0 | 158,-0.0 | 0.426 | 105.0-132.3 -87.9 -3.3 | | -11.4 | 49.4 | 16.3 | | |
| 23 | 27 | A | C S < S+ | | 0 | 0 | 112 | -3,-1.2 | -5,-0.1 | -6,-0.2 | -6,-0.0 | 0.730 | 80.2 98.1 62.8 28.1 | | -7.6 | 49.4 | 16.9 | | |

Amino
Acids

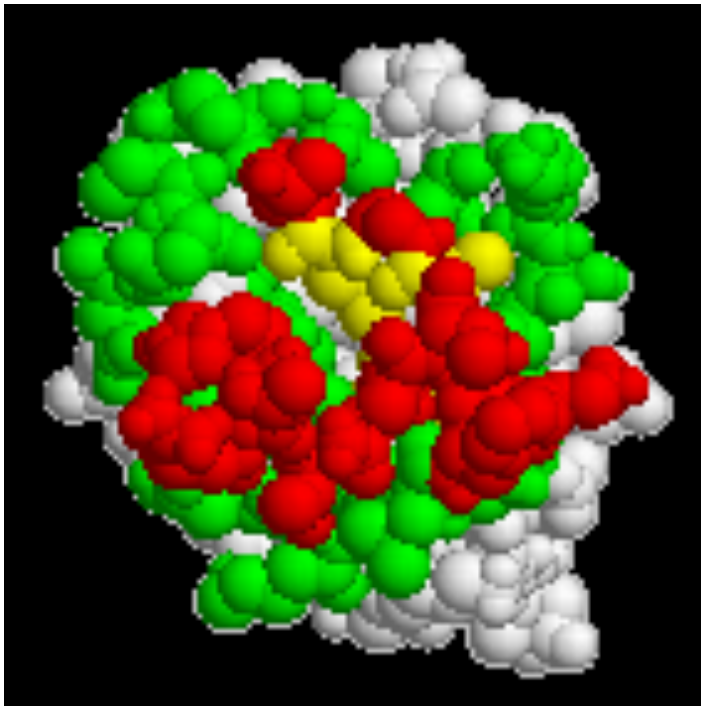
Secondary
Structure

Solvent
Accessibility



Solvent Accessibility

Size of the area of an amino acid that is exposed to solvent (water).

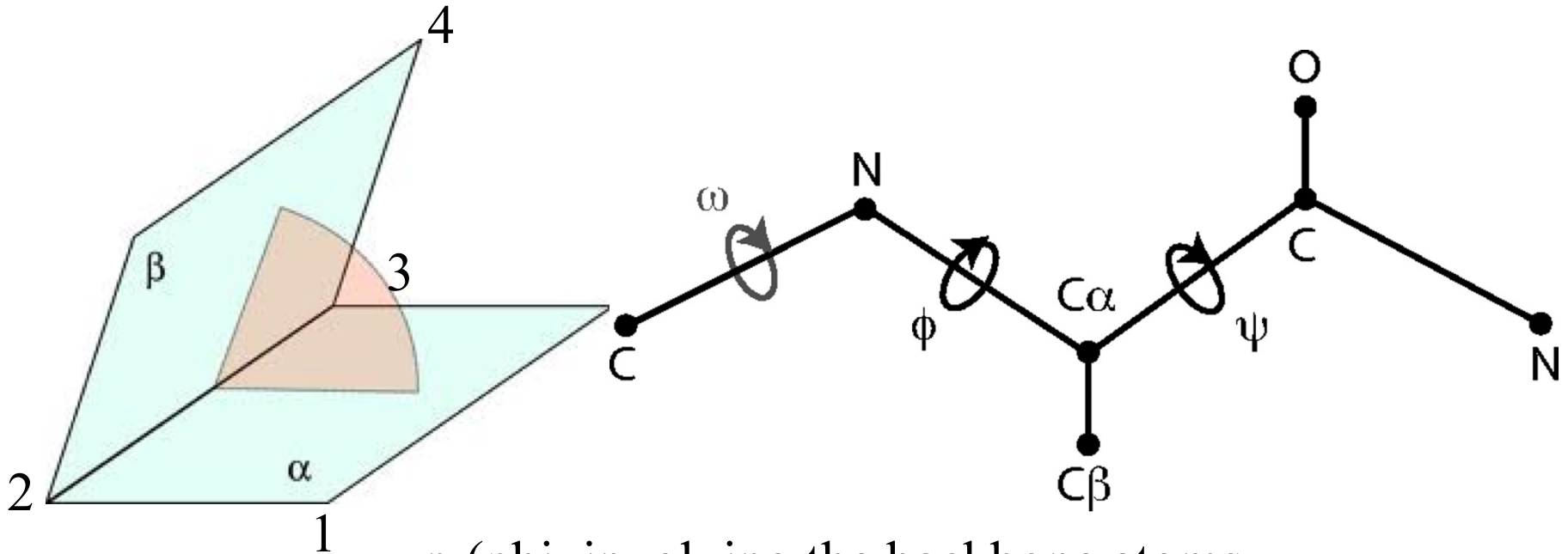


Maximum solvent accessible area for each amino acid is its whole surface area.

Hydrophobic residues like to be Buried inside (interior).

Hydrophilic residues like to be exposed on the surface.

Dihedral / Torsional Angle

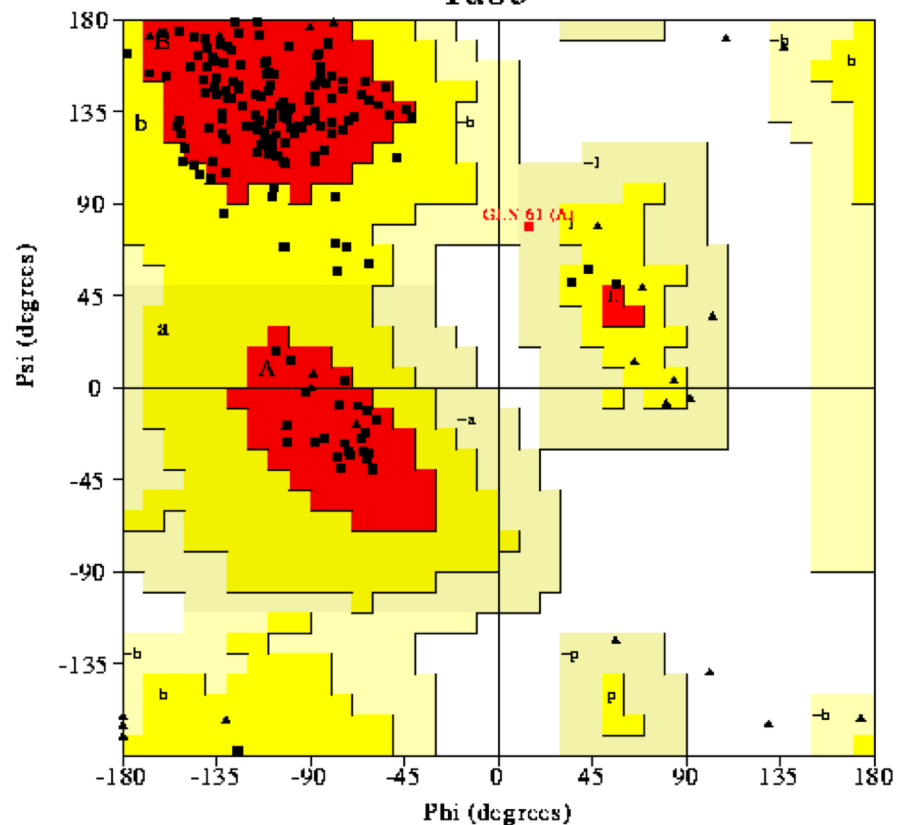


ϕ (phi, involving the backbone atoms C'-N-C α -C'), ψ (psi, involving the backbone atoms N-C α -C'-N)

- http://en.wikipedia.org/wiki/Dihedral_angle

Ramachandran Plot

1abc



Plot statistics

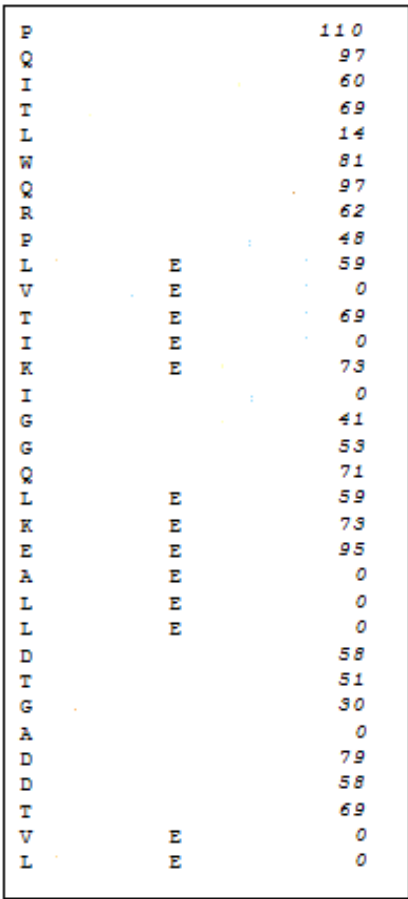
| | | |
|---|-----|--------|
| Residues in most favoured regions [A, B, I] | 143 | 69.9% |
| Residues in additionally allowed regions [a, b, i, p] | 15 | 9.4% |
| Residues in generously allowed regions [-a, -b, -i, -p] | 1 | 0.6% |
| Residues in disallowed regions | 0 | 0.0% |
| Number of non-glycine and non-proline residues | 159 | 100.0% |
| Number of end residues (excl. Gly and Pro) | 5 | |
| Number of glycine residues (shown as triangles) | 26 | |
| Number of proline residues | 15 | |
| Total number of residues | 205 | |

Based on an analysis of 118 structures of resolution of at least 2.0 Angstroms and R-factor no greater than 20%, a good quality model would be expected to have over 90% in the most favoured regions.

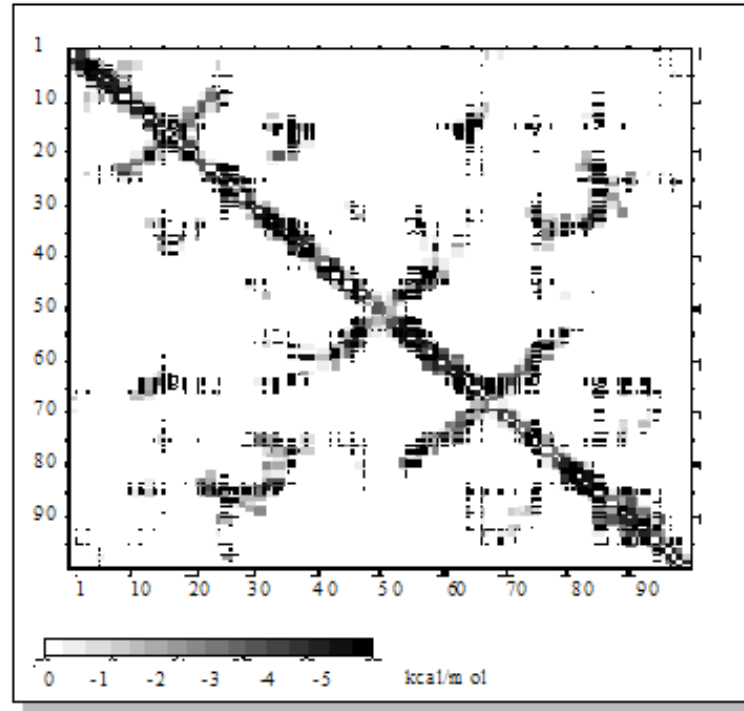
Project Groups

- 19 students?
- Form 4 groups (4-5 students per group)

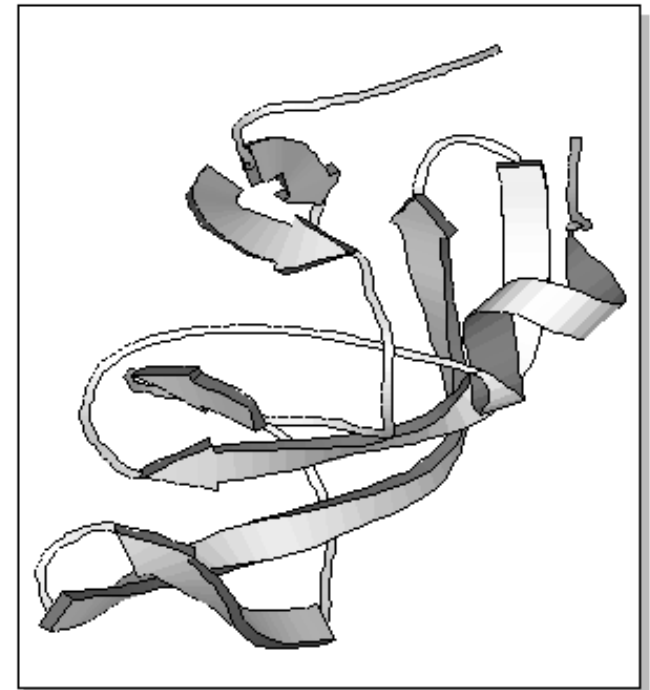
Protein Structure 1D, 2D, 3D



1D



2D



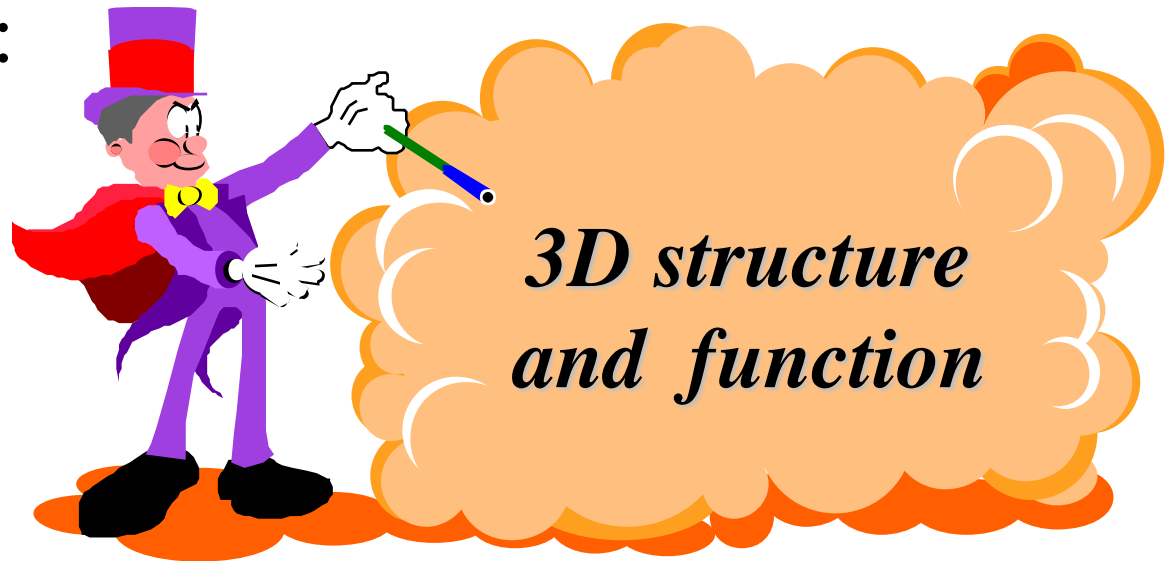
3D

Goal of Structure Prediction

- Epstein & Anfinsen, 1961:
sequence uniquely determines structure

- INPUT: sequence

- OUTPUT:



This is a Nobel Prize Winning Problem!!!

CASP – Olympics of Protein Structure Prediction

- Critical Assessment of Techniques of Protein Structure Prediction
- 1994, 1996, 1998, 2000, 2002, 2004, 2006, 2008, 2010, 2012, 2014, 2016, 2018
- Blind Test, Independent Evaluation

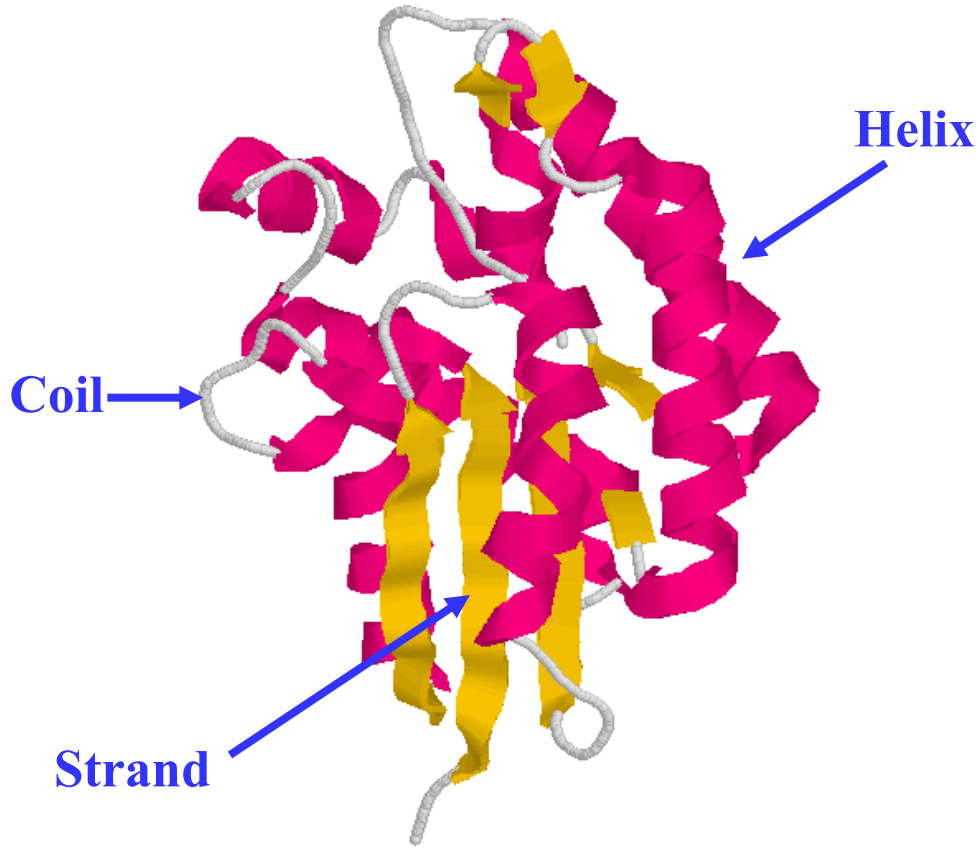


- **CASP13** (<http://predictioncenter.org/casp13/index.cgi>)

CASP13 Demo

- <http://predictioncenter.org/casp13/index.cgi>

1D: Secondary Structure Prediction



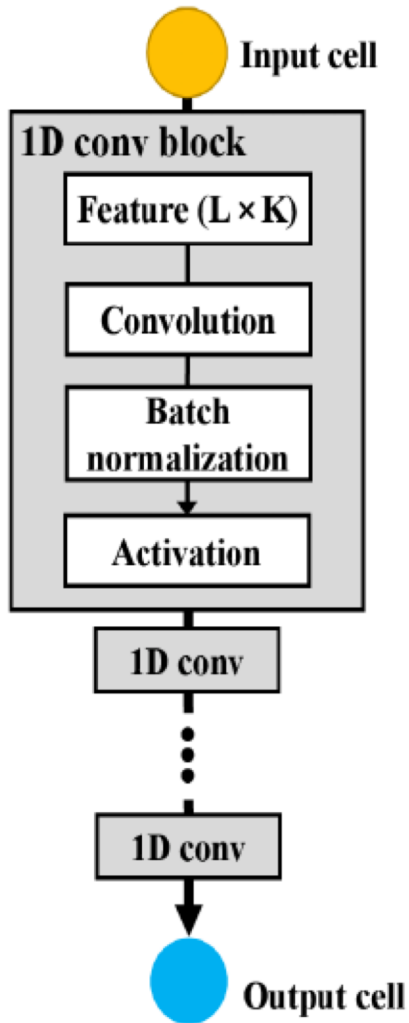
MWLKKFGINLLIGQSV...

Neural Networks /
Deep Learning
+ Alignments

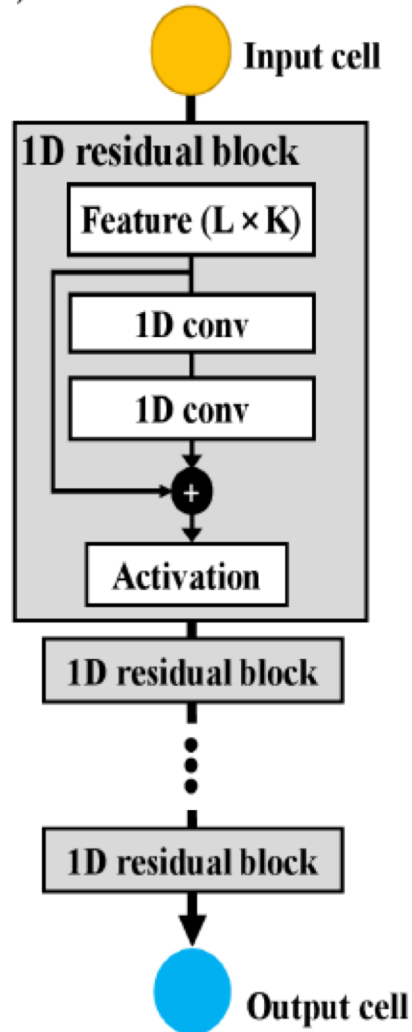
CCCCHHHHCCCCSSSS...

Deep Learning

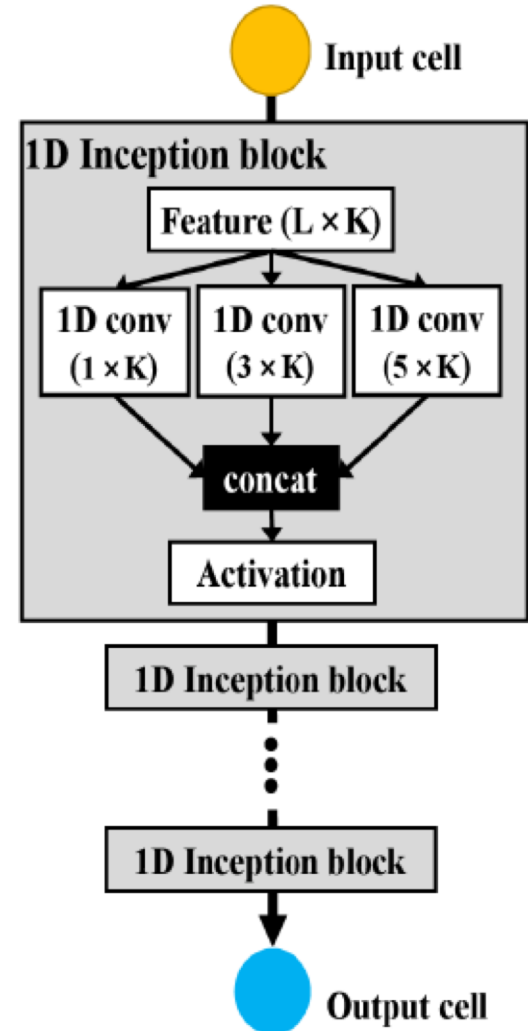
(A) CNN



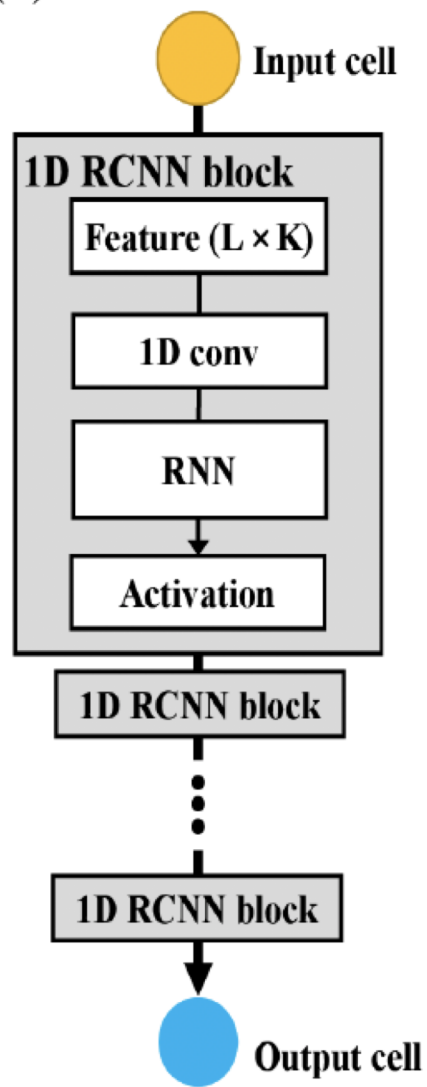
(B) ResNet



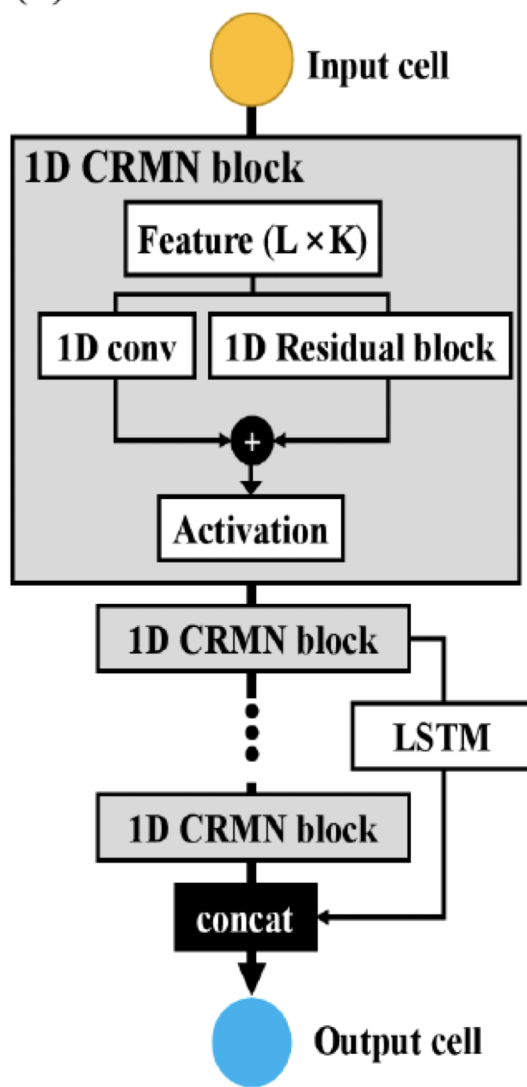
(C) InceptionNet



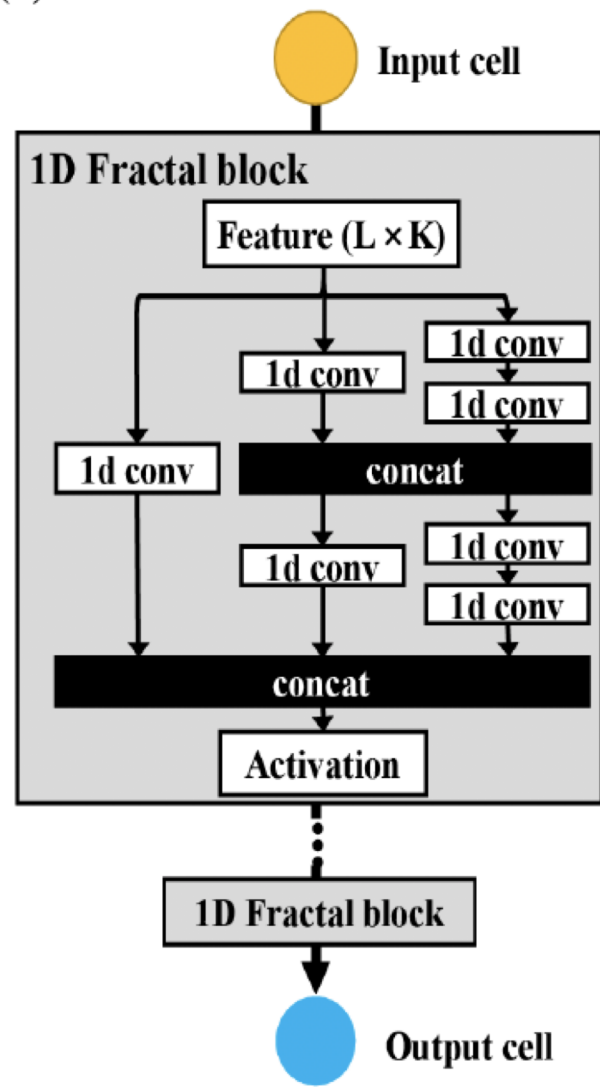
(D) RCNN



(E) CRMN

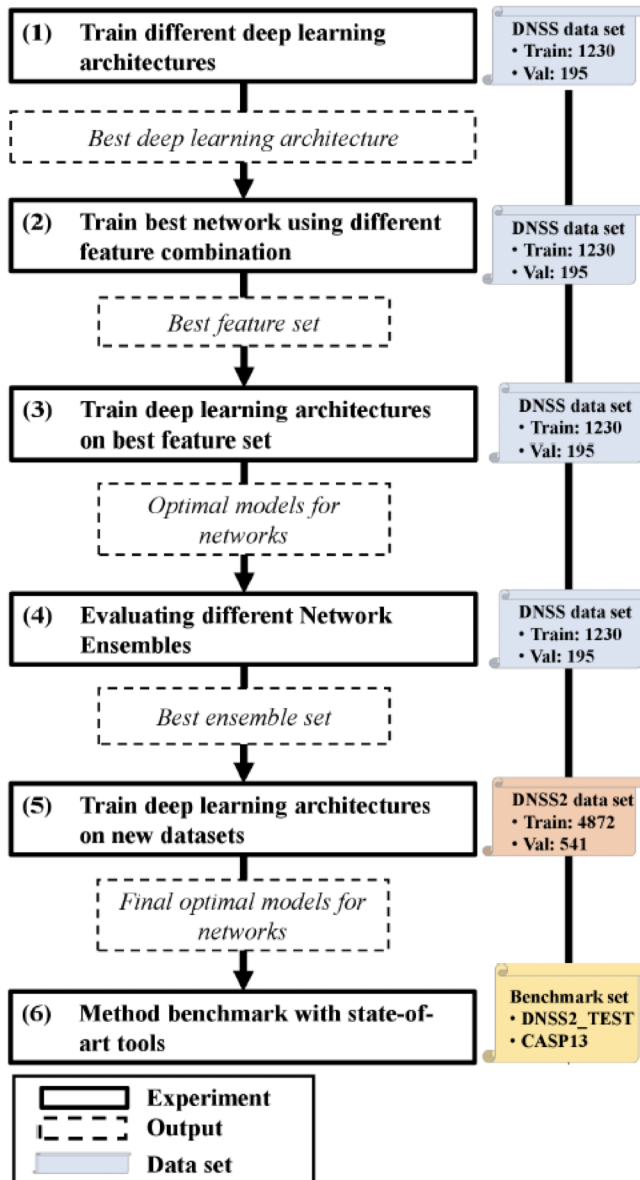


(F) FractalNet

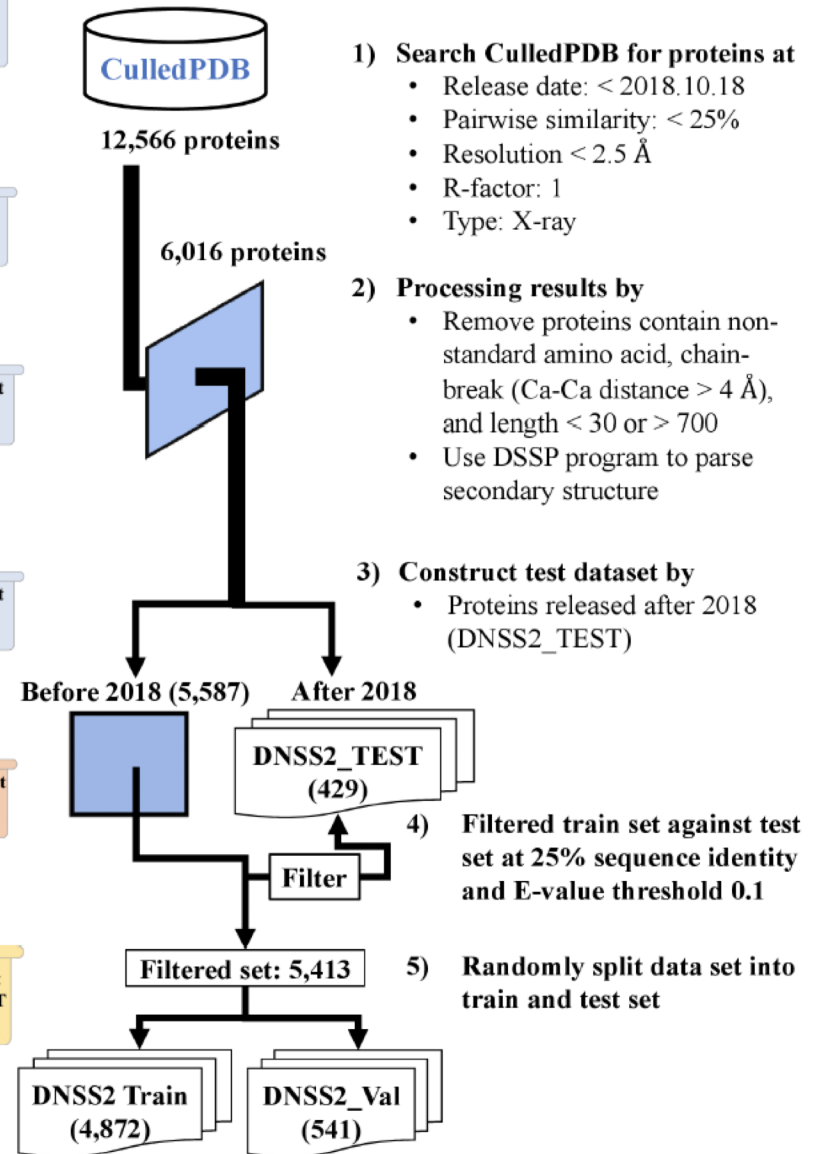


Machine Learning Workflow

(A)



(B)



| Method | Q3(%) | Sov(%) |
|---------------------------|--------------|---------------|
| DNSS2_CNN | 80.29 | 72.1 |
| DNSS2_RCNN | 81.83 | 73.97 |
| DNSS2_ResNet | 81.53 | 73.71 |
| DNSS2_CRMN | 81.91 | 73.37 |
| DNSS2_FractalNet | 82.02 | 73.8 |
| DNSS2_InceptionNet | 82.74 | 75.3 |
| DNSS2 | 83.84 | 75.5 |

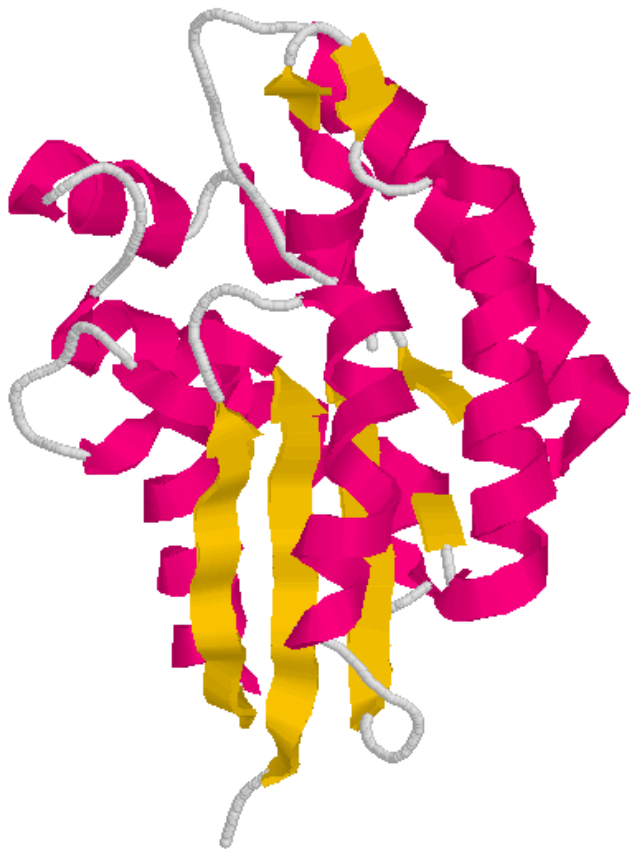
Table 3. Performance of the six different deep learning architectures (CNN, RCNN, ResNet, CRMN, FractalNet, and InceptionNet) and their ensemble (DNSS2) on DNSS1 validation dataset and the updated protein sequence database.

| Method | All | | TBM | | FM | |
|----------|-----------|------------|-----------|------------|-----------|------------|
| | Q3 (%) | SOV (%) | Q3 (%) | SOV (%) | Q3 (%) | SOV (%) |
| SSPro5.2 | 76.73 | 69.94 | 78.16 | 71.32 | 76.12 | 70.88 |
| PSSpred | 78.8 | 67.85 | 81.32 | 72.11 | 76.99 | 64.55 |
| MUFOLD | 79.58 | 71.74 | 79.71 | 74.13 | 79.8 | 70.79 |
| DeepCNF | 80.24 | 69.5 | 82.34 | 73.68 | 78.36 | 65.55 |
| PSIPRED | 80.7 | 72 | 83.67 | 76.72 | 78.41 | 68.14 |
| SPIDER3 | 81.73 | 74.39 | 84.84 | 78.31 | 78.89 | 71.1 |
| Porter5 | 82.07 | 74.61 | 84.79 | 78.98 | 79.42 | 70.3 |
| DNSS1 | 77.06 | 70.40 | 79.48 | 73.58 | 75.46 | 68.79 |
| DNSS2 | 82.2 | 73.03 | 85.37 | 76.98 | 79.82 | 70.56 |

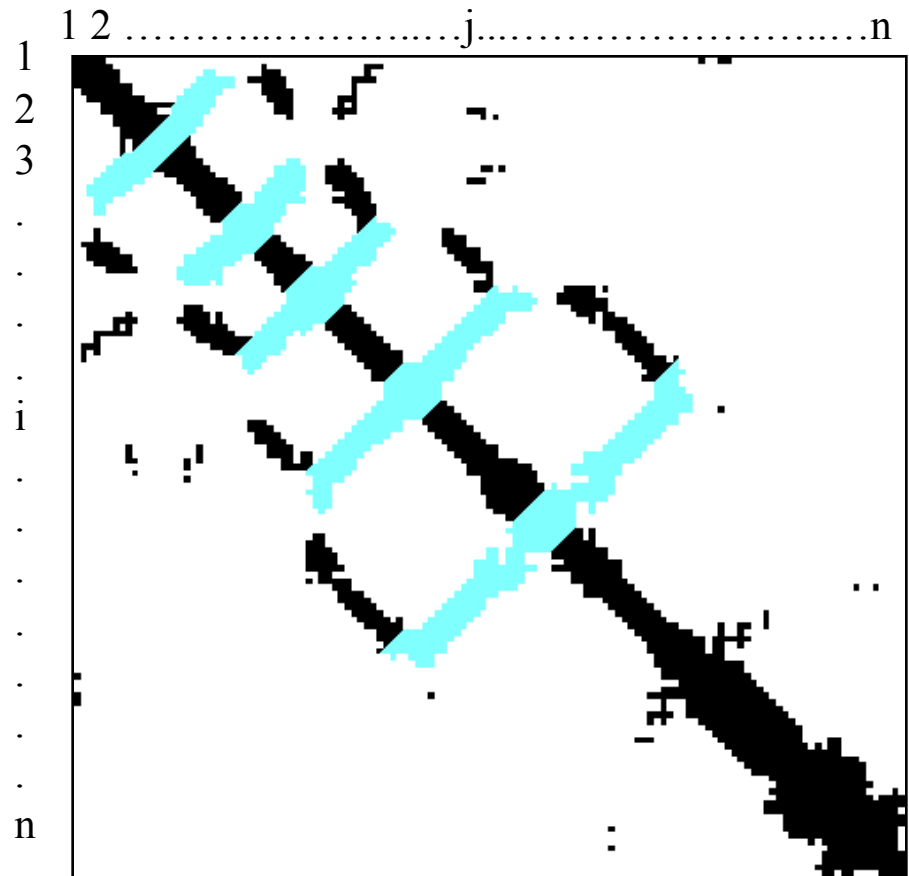
Table 5. Comparison of methods on the CASP13 dataset in terms of all CASP13 targets, template-based targets, and template-free targets.

2D: Contact Map Prediction

3D Structure



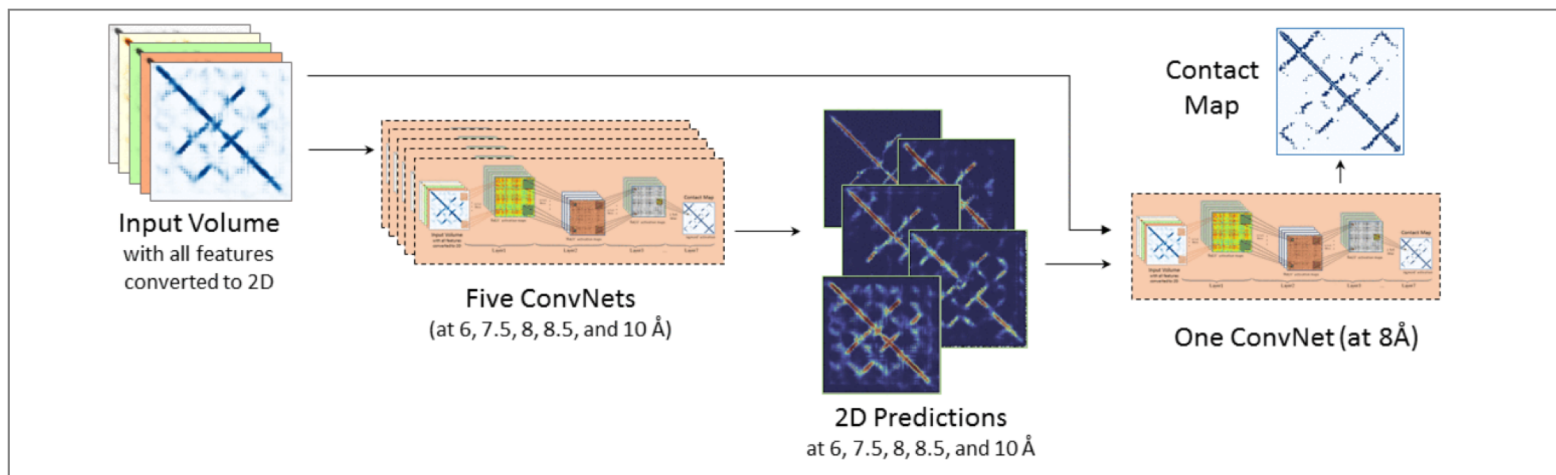
2D Contact Map



Distance Threshold = 8Å°

Cheng, Randall, Sweredoski, Baldi. *Nucleic Acid Research*, 2005

DNCON2: Protein Contact Prediction Using Deep CNN



Submit Your Job

[Please submit maximum two sequences at a time]

Job Id

E-mail

Sequence

Run DNCON2

Download DNCON2 code [here](#).

Download DNCON2's predictions for CASP 10, 11, and 12 datasets [here](#).

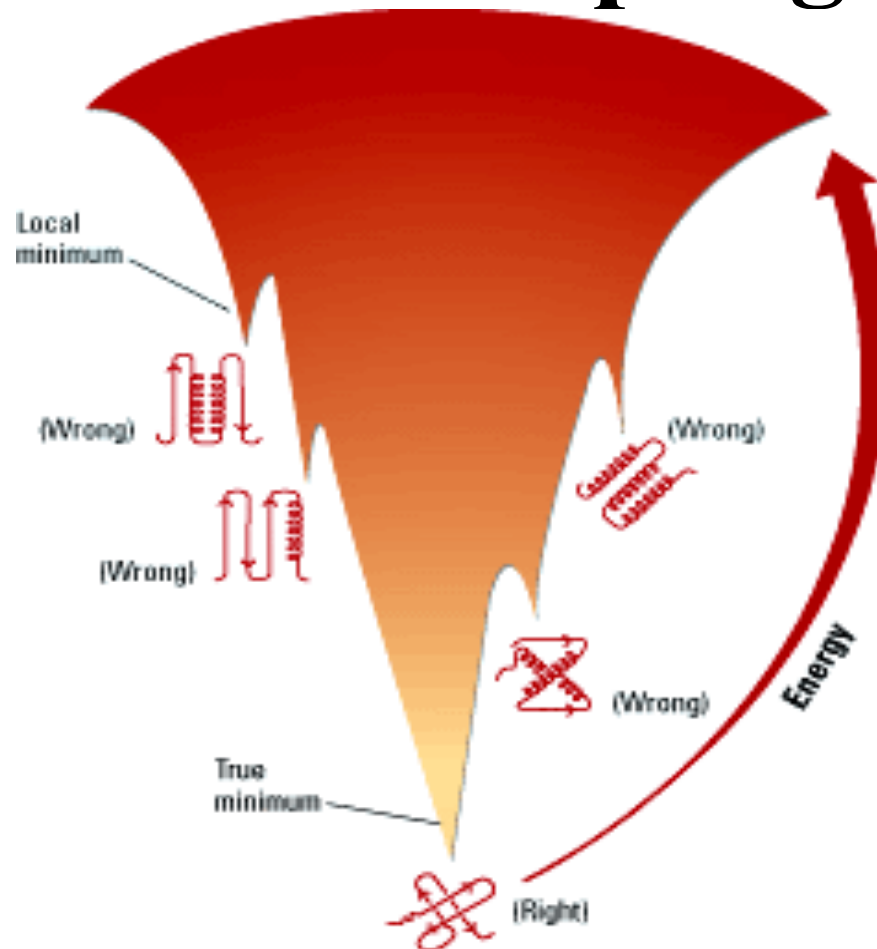
Download DNCON2's training/testing dataset (fastas and lists) [here](#).

Contact Prediction

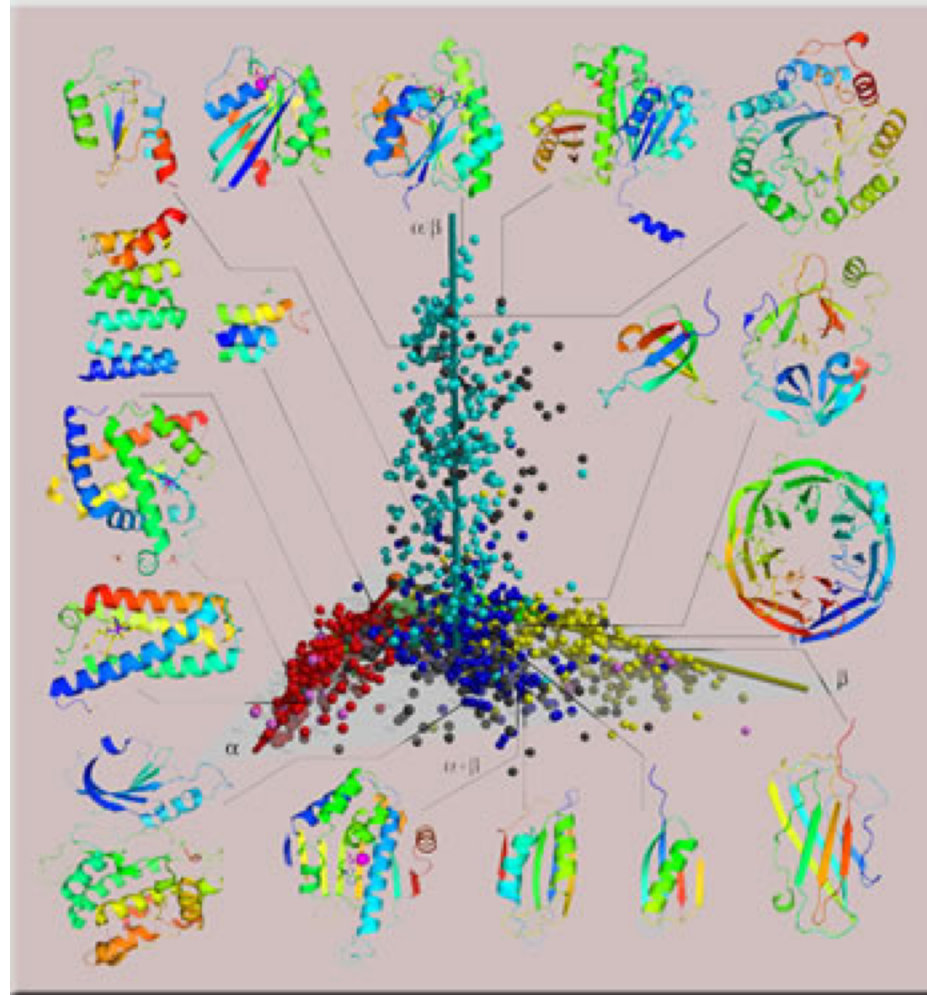
- PISCOV: <http://bioinfadmin.cs.ucl.ac.uk/downloads/PSICOV/>
- DNCON2: <https://github.com/multicom-toolbox/DNCON2>
- DeepCov <https://github.com/psipred/DeepCov>

Protein tertiary structure prediction is a space sampling / simulation / optimization problem.

Protein Energy Landscape & Free Sampling



Protein Structure Space & Target Sampling

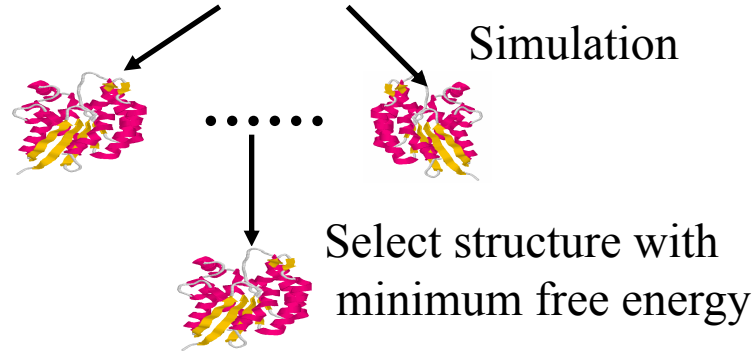


Two Approaches for 3D Structure Prediction

• Ab Initio Structure Prediction

Physical force field – protein folding
Contact/distance map - reconstruction

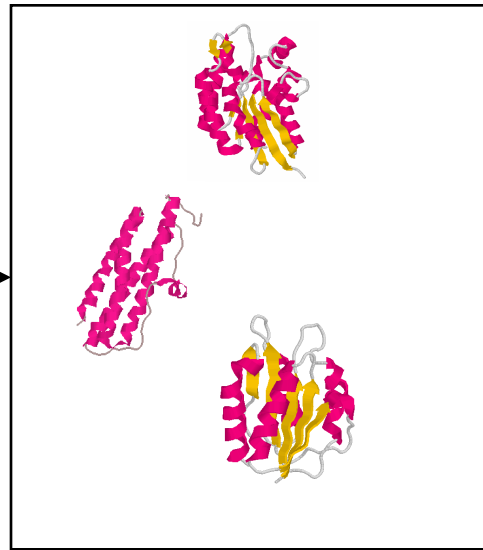
MWLKKFGINLLIGQSV...



• Template-Based Structure Prediction

Query protein

MWLKKFGINKH...



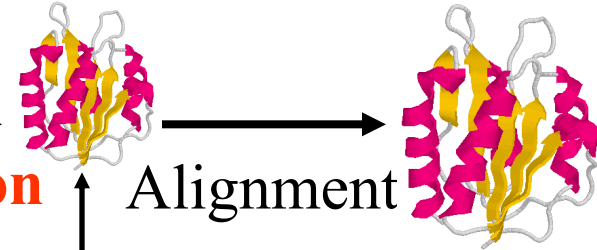
Protein Data Bank

Fold

Recognition

Template

Alignment



Template-Based Structure Prediction \leftrightarrow KNN Learning

1. Template identification
2. Query-template alignment
3. Model generation
4. Model evaluation
5. Model refinement

Notes: if template is easy to identify, it is often called **comparative Modeling or homology** modeling. If template is hard to identify, it is often called **fold recognition**.

TARGET

TEMPLATE

ASILPKRLFGNCEQTSDEGLK
IERTPLVPHISAQNVCLKIDD
VPERLIPERASFQWMNDK



ASILPKRLFGNCEQTSDEGLK IERTPLVPHISAQNVCLKIDD VPERLIPE
MSVIPKRLYG NCEQTSEEAIRIEDSPIV --- TADLVCLKIDEIPERLVGE



Copy
Loop Modeling
Optimization

How to find templates?
How to get alignments?

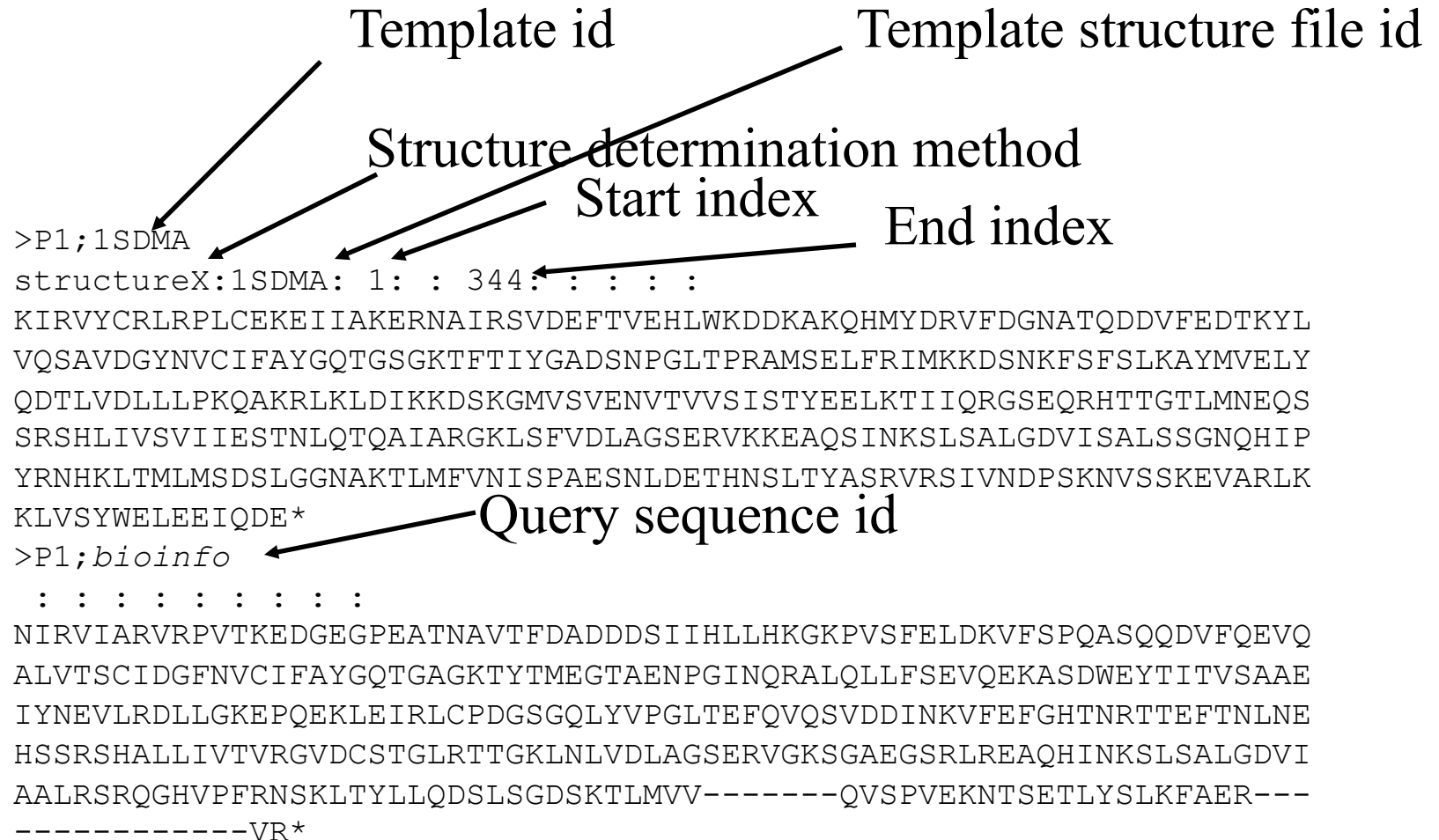
Modeller

- Need an alignment file between query and template sequence in the PIR format
- Need the structure (atom coordinates) file of template protein
- You need to write a simple script (Python for version 8.2) to tell how to generate the model and where to find the alignment file and template structure file.
- Run Modeller on the script. Modeller will automatically copy coordinates and make necessary adjustments to generate a model.

How to Get Templates and Alignments

- PSI-BLAST
- Hhblits
- Sequence/profile databases curated from the Protein Data Bank (PDB)

An PIR Alignment Example



Structure File Example (1SDMA.atm)

| | | | | | | | | | | |
|------|----|-----|-----|---|---------|--------|---------|------|-------|---|
| ATOM | 1 | N | LYS | 1 | -3.978 | 26.298 | 113.043 | 1.00 | 31.75 | N |
| ATOM | 2 | CA | LYS | 1 | -4.532 | 25.067 | 113.678 | 1.00 | 31.58 | C |
| ATOM | 3 | C | LYS | 1 | -5.805 | 25.389 | 114.448 | 1.00 | 30.38 | C |
| ATOM | 4 | O | LYS | 1 | -6.887 | 24.945 | 114.072 | 1.00 | 32.68 | O |
| ATOM | 5 | CB | LYS | 1 | -3.507 | 24.446 | 114.631 | 1.00 | 34.97 | C |
| ATOM | 6 | CG | LYS | 1 | -3.743 | 22.970 | 114.942 | 1.00 | 36.49 | C |
| ATOM | 7 | CD | LYS | 1 | -3.886 | 22.172 | 113.644 | 1.00 | 39.52 | C |
| ATOM | 8 | CE | LYS | 1 | -3.318 | 20.766 | 113.761 | 1.00 | 41.58 | C |
| ATOM | 9 | NZ | LYS | 1 | -1.817 | 20.761 | 113.756 | 1.00 | 43.48 | N |
| ATOM | 10 | N | ILE | 2 | -5.687 | 26.161 | 115.522 | 1.00 | 26.16 | N |
| ATOM | 11 | CA | ILE | 2 | -6.867 | 26.500 | 116.302 | 1.00 | 22.75 | C |
| ATOM | 12 | C | ILE | 2 | -7.887 | 27.226 | 115.439 | 1.00 | 21.35 | C |
| ATOM | 13 | O | ILE | 2 | -7.565 | 28.200 | 114.770 | 1.00 | 20.95 | O |
| ATOM | 14 | CB | ILE | 2 | -6.513 | 27.377 | 117.523 | 1.00 | 21.68 | C |
| ATOM | 15 | CG1 | ILE | 2 | -5.701 | 26.563 | 118.526 | 1.00 | 21.13 | C |
| ATOM | 16 | CG2 | ILE | 2 | -7.782 | 27.875 | 118.200 | 1.00 | 18.96 | C |
| ATOM | 17 | CD1 | ILE | 2 | -5.368 | 27.325 | 119.787 | 1.00 | 21.39 | C |
| ATOM | 18 | N | ARG | 3 | -9.120 | 26.737 | 115.461 | 1.00 | 22.04 | N |
| ATOM | 19 | CA | ARG | 3 | -10.214 | 27.327 | 114.693 | 1.00 | 23.95 | C |
| ATOM | 20 | C | ARG | 3 | -10.783 | 28.563 | 115.400 | 1.00 | 22.82 | C |
| ATOM | 21 | O | ARG | 3 | -10.771 | 28.645 | 116.629 | 1.00 | 22.62 | O |
| ATOM | 22 | CB | ARG | 3 | -11.327 | 26.290 | 114.510 | 1.00 | 26.34 | C |
| ATOM | 23 | CG | ARG | 3 | -11.351 | 25.586 | 113.161 | 1.00 | 30.68 | C |
| ATOM | 24 | CD | ARG | 3 | -10.004 | 25.034 | 112.771 | 1.00 | 35.43 | C |
| ATOM | 25 | NE | ARG | 3 | -10.104 | 24.072 | 111.672 | 1.00 | 43.37 | N |
| ATOM | 26 | CZ | ARG | 3 | -10.575 | 24.350 | 110.458 | 1.00 | 46.04 | C |
| ATOM | 27 | NH1 | ARG | 3 | -10.997 | 25.572 | 110.168 | 1.00 | 48.68 | N |
| ATOM | 28 | NH2 | ARG | 3 | -10.627 | 23.400 | 109.532 | 1.00 | 48.37 | N |
| ATOM | 29 | N | VAL | 4 | -11.278 | 29.524 | 114.630 | 1.00 | 20.49 | N |
| ATOM | 30 | CA | VAL | 4 | -11.853 | 30.724 | 115.225 | 1.00 | 17.59 | C |
| ATOM | 31 | C | VAL | 4 | -13.082 | 31.211 | 114.471 | 1.00 | 18.31 | C |
| ATOM | 32 | O | VAL | 4 | -13.030 | 31.446 | 113.264 | 1.00 | 16.37 | O |
| ATOM | 33 | CB | VAL | 4 | -10.834 | 31.872 | 115.272 | 1.00 | 19.94 | C |
| ATOM | 34 | CG1 | VAL | 4 | -11.512 | 33.168 | 115.759 | 1.00 | 15.64 | C |
| ATOM | 35 | CG2 | VAL | 4 | -9.668 | 31.489 | 116.168 | 1.00 | 15.45 | C |

Modeller Python Script (bioinfo.py)

```
# Homology modelling by the automodel class
```

```
from modeller.automodel import * # Load the automodel class
```

```
log.verbose() # request verbose output
```

```
env = environ() # create a new MODELLER environment to build this model in
```

```
# directories for input atom files
```

```
env.io.atom_files_directory = './../atom_files'
```

```
a = automodel(env,
```

```
   alnfile = 'bioinfo.pir', # alignment filename
```

```
    knowns = '1SDMA', # codes of the templates
```

```
    sequence = 'bioinfo') # code of the target
```

```
a.starting_model= 1 # index of the first model
```

```
a.ending_model = 1 # index of the last model
```

```
    # (determines how many models to calculate)
```

```
a.make() # do the actual homology modelling
```

Where to find structure file

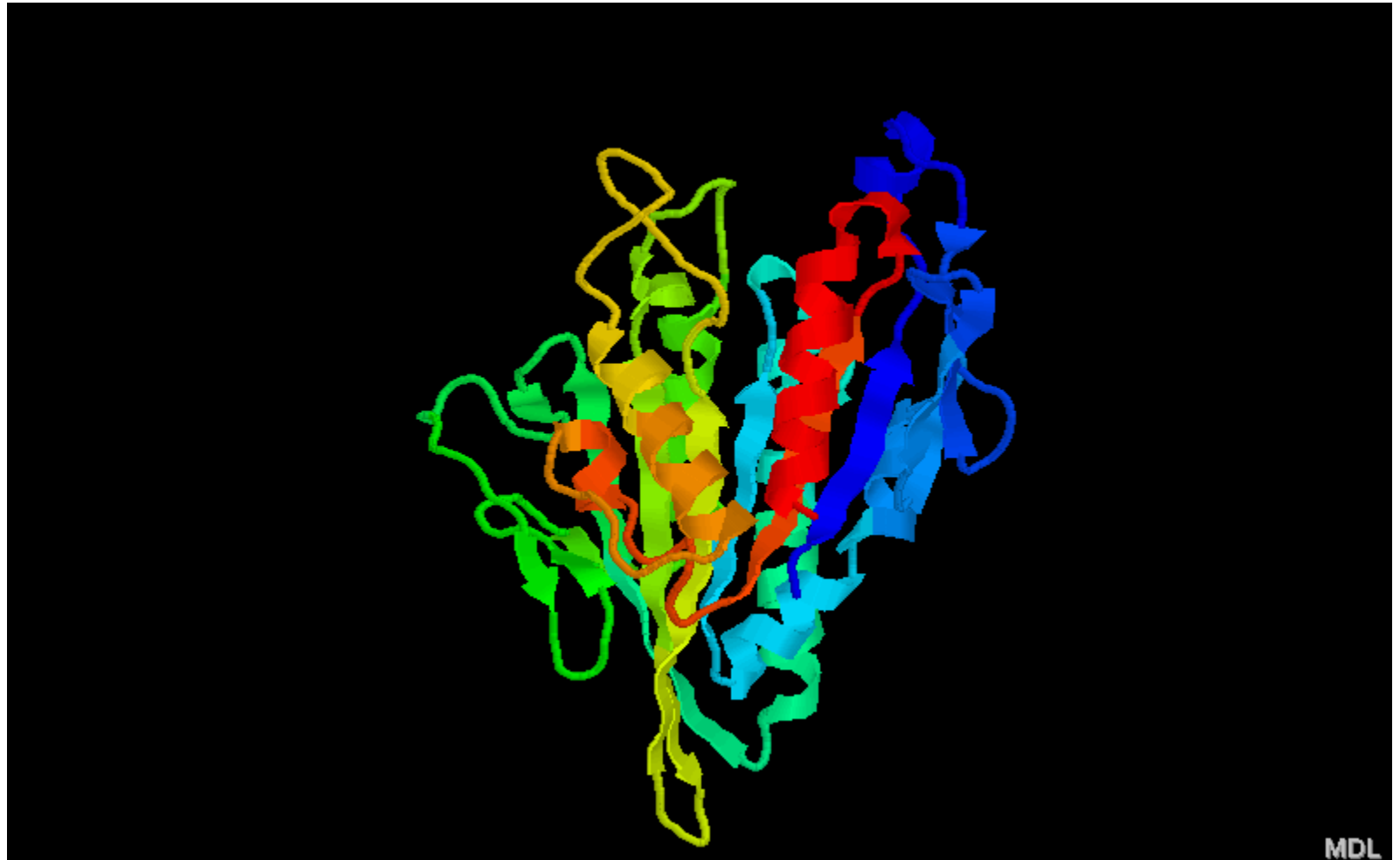
PIR alignment file name

Template structure file id

Query sequence id

Output Example

Command: mod8v2 bioinfo.py



Template Based Modeling Methods

- Comparative Protein Modeling by Satisfaction of Spatial Restraints by Andrej Sali and Tom L. Blundell
- 3D Model is obtained by satisfying spatial restraints derived from alignment with a known structure, which are expressed as probability density functions (pdfs) of the restraints.
- Pdfs serve as an objective function for optimization

Probability Density Functions of Features

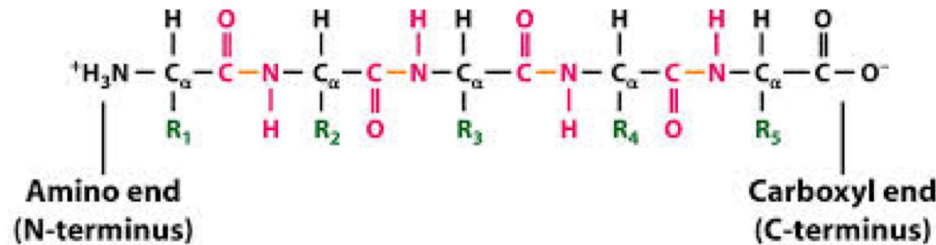


Figure 3-3b
Molecular Cell Biology, Sixth Edition
© 2008 W. H. Freeman and Company

- Ca – Ca distances
- Main-chain N-O distance
- Main-chain dihedral angles
- Side-chain dihedral angles
- A protein pdf is a combination of individual pdfs of features of the whole protein

Optimization Procedure

- Objective: the pdf of a protein derived from restraints extracted from templates and alignments
- Initial input: initial (x, y, z) of each residue satisfying bond length / angle restraints
- Optimization: adjust x, y, z to maximize the pdf (i.e. probability), i.e. reduce the violations of feature restraint as much as possible

Topic 1 – Template Based Modeling

- CASP12/CASP13 TBM targets
- Known templates at CASP12/CASP13 web sites
- Develop a homology-based algorithm / tool to build models from templates (gradient descent algorithm preferred)
- Assess the quality of models
- Implement from scratch
- **Form your group**

Feature Restraints from Template Data

- Given the information (a distance between two amino acids) in template, what can we know about the target?
- Feature constraint is represented as conditional distribution. E.g. $P(\text{ca-ca distance in target} \mid \text{ca-ca distance in template, residue type 1, residue type 2, ...})$, $P(\text{psi angle of a residue in target} \mid \text{psi angle of an equivalent residue in template, ...})$

How to quantify the information? Function Fitting from Known Data - Learning

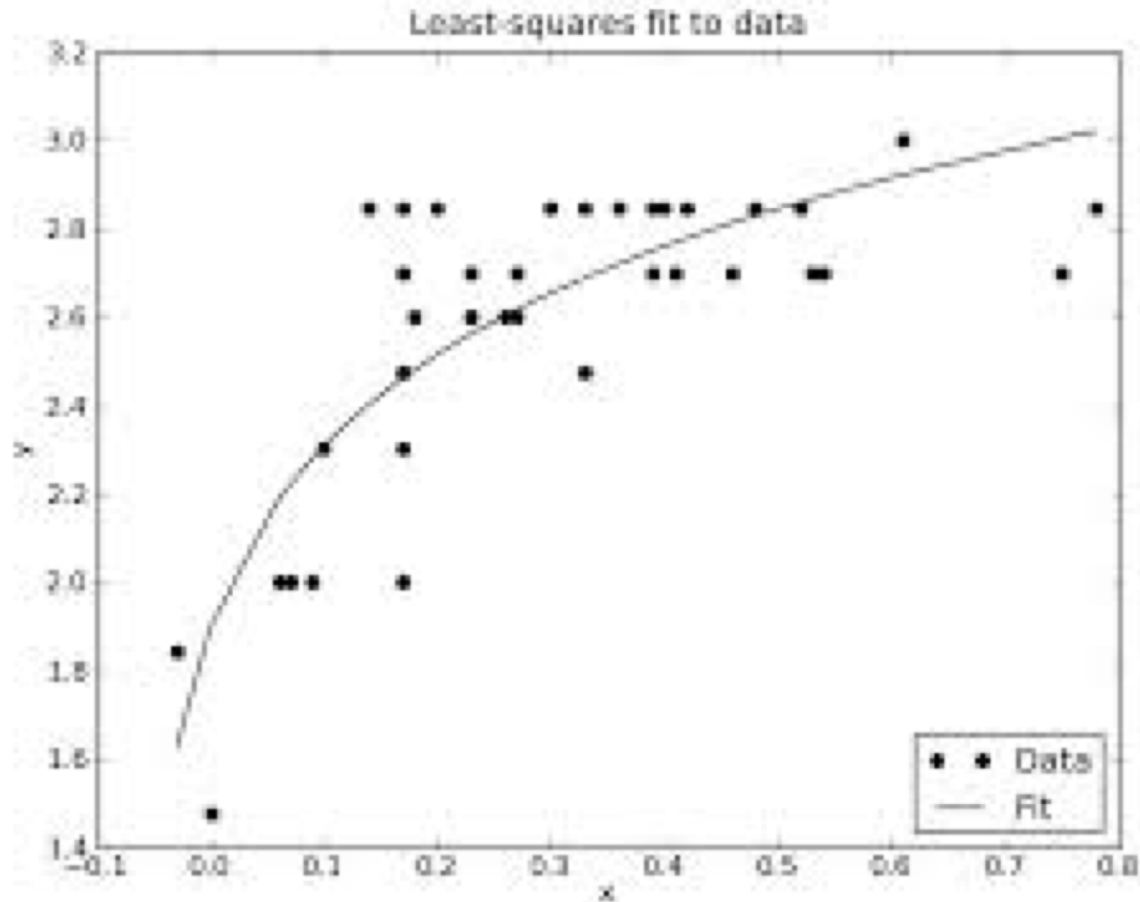
- A probability density function: $P(y|x, a, b, c, \dots)$
- Distribution form: normal distribution?
- Estimate the mean and standard deviation?
- Get some known data (template, target structures)
- Fitting algorithm: *Levenberg-Marquardt* algorithm for non-constrained least-squares fitting of a non-linear multidimensional model

An Example of Generating a pdf for one feature (phi angle)

| Residue A in target | Residue B in template | Angle in Template | Angle in Target |
|---------------------|-----------------------|-------------------|------------------|
| A | C | 50 | 58, 60, 49, ... |
| A | C | 70 | 67, 82, 87 |
| A | K | 10 | 9.5, 11, 10.8... |
| ... | ... | ... | ... |

A database of 17 family alignments including 80 proteins was constructed to obtain feature statistics (**training/fitting**).

Levenberg-Marquardt algorithm



**Calculate mean
from the function**

**Estimate standard
deviation**

| | | |
|----|------------|---|
| 1 | r | Amino acid residue type |
| 2 | Φ | Main-chain dihedral angle Φ |
| 3 | Ψ | Main-chain dihedral angle Ψ |
| 4 | t | Secondary structure class of a residue |
| 5 | M | Main-chain conformation class of a residue |
| 6 | α | Fractional content of residues in the main-chain conformation class A |
| 7 | χ_i | Side-chain dihedral angle χ_i , $i = 1, 2, 3, 4$ |
| 8 | c_i | Side-chain dihedral angle χ_i class, $i = 1, 2, 3, 4$ |
| 9 | a | Residue solvent accessibility |
| 10 | \bar{a} | Average accessibility of two residues in one protein |
| 11 | s | Residue neighbourhood difference between two proteins |
| 12 | \bar{s} | Average residue neighbourhood difference between two proteins |
| 13 | i | Fractional sequence identity between two proteins |
| 14 | d | C $^{\alpha}$ -C $^{\alpha}$ distance |
| 15 | Δd | Difference between two C $^{\alpha}$ -C $^{\alpha}$ distances in two proteins |
| 16 | h | Main-chain N-O distance |
| 17 | Δh | Difference between two main-chain N-O distances in two proteins |
| 18 | b | Average residue B_{iso} |
| 19 | R | Resolution of X-ray analysis |
| 20 | g | Distance of a residue from a gap in alignment |
| 21 | \bar{g} | Average distance of a residue from a gap |

Commons Features

Side Chain & Main Chain

- Main-chain and side-chain modeling can be separated or carried out simultaneously
- Many tools model main chain first and then use SCWRL to add side chains in order to simplify the problem.
- All-atom modeling is more complex and time consuming, but can be more accurate sometime.

Usefulness of Features

- The most useful pdf is the one that predicts the unknown feature most accurately, measured by the entropy of a pdf.
- Two kinds of features: (1) generic features for all proteins and (2) features specific for the target protein

Stereochemical Restraints

(Generic for any protein)

- Obtained from sequence of a protein
- Bond distance, bond angle, planarity of peptide groups, side-chain rings, chiralities of Ca atoms and side-chains, van der Waals volumes (radii values)
- Mean value and standard deviations for bond lengths, bond angles, and dihedral angles are obtained from GROMOS86

Bond Length and Angles (harmonic model)

The classical harmonic model for the bond length between two atoms gives the vibrational potential energy of the bond as:

$$E(b) = \frac{1}{2}c(b - b_o)^2. \quad (19)$$

$$p^b(b) = \frac{1}{\sigma_b \sqrt{2\pi}} \exp \left[-\frac{1}{2} \left(\frac{b - \bar{b}}{\sigma_b} \right)^2 \right] = N(\bar{b}, \sigma_b).$$

Van der Waals Repulsion (only non-harmonic feature)

(ii) *van der Waals repulsion*

van der Waals repulsion is the only stereochemical feature which is not described by the harmonic model. Instead, the following pdf is used for two atoms:

$$p^v(d) = c \cdot \begin{cases} N(d_o, \sigma_w); & d \leq d_o \\ \frac{1}{\sigma_w \sqrt{2\pi}}; & d_o < d < d_{\max}, \end{cases} \quad (22)$$

where d is the distance between the two atoms, d_o is the sum of their van der Waals radii and σ_w is the standard deviation of the Gaussian part of the whole pdf (usually 0.05 Å). d_{\max} is the maximal possible linear dimension of a protein and constant c is chosen so that $p^v(d)$ integrates to 1. This pdf does not differentiate between contact distances larger than d_o , but it does select against distances smaller than d_o . This is achieved by imposing a repulsive harmonic potential on atoms that are less than d_o apart.

Ca-Ca Distance Features (protein specific)

$$p^d(d|\bar{g}, i, \bar{a}', d') = \frac{1}{\sigma(\bar{g}, i, \bar{a}', d')\sqrt{2\pi}} \times \exp\left[-\frac{1}{2}\left(\frac{d-d'}{\sigma(\bar{g}, i, \bar{a}', d')}\right)^2\right]$$

Standard deviation depends on solvent accessibility, gaps of alignment, and sequence identity.

Combine pdfs of a Feature (Ca-Ca distance) from Multiple Templates

- Weighted sum of the same type of pdfs from multiple known structures

The last step in the derivation of the feature pdf is to include the van der Waals restraint. Since all stereochemical restraints have to be satisfied in all structures, these restraints are multiplied into the feature pdf and we obtain the final feature pdf:

$$p^D(d) = [\omega_1 p_1^d(d) + \omega_2 p_2^d(d)] p^v(d).$$

Derivation of a molecular pdf from individual feature pdfs

- Combine all feature pdfs into a molecular pdf $P = \prod_i p^F(f_i)$. (34)
- 3D structure of a protein is uniquely determined if a sufficient large number of its features, f_i , are specified
- The goal is to find the 3D structure that is consistent with the most probable values of individual features f_i , i.e. to maximize the molecular pdf or its logarithm.

Optimization

- Optimize the logarithm of molecular pdf – the objective function

F.
$$F = -\ln(P), \quad (35)$$

- All the features of the molecular pdf is expressed in terms of atomic Cartesian coordinates (x, y, z)
- F is more suitable for optimization because multiplication is converted into addition and the problem of floating point overflow is smaller for F.

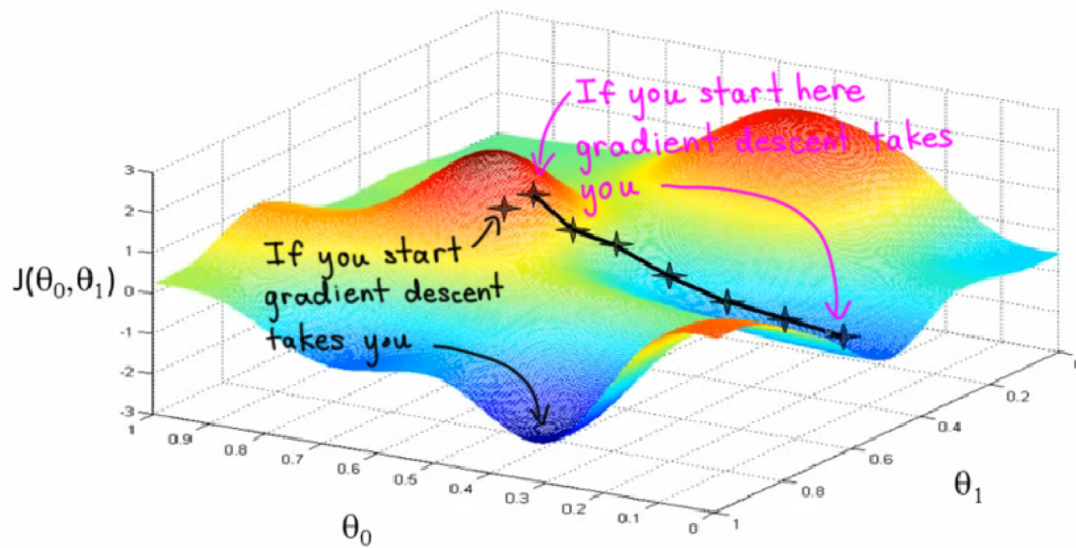
Successive Optimization

- The optimum of the molecular pdf is found by successive optimization of increasingly more complex target function till the whole molecular pdf.
- From local restraints to long-range restraints to all the restraints
- Restraints is ordered by the sequence distance between atoms / residues (1, 2, ...N-1), N is the sequence length.
- Successively adding restraints with \leq sequence distance i at each step i .

Initial Conformation of Step i

- At step 1, initial conformation can be an extended chain, or a conformation derived from the extended chain by rotation of dihedral angles
- At step i , the initial conformation is the final conformation of step $i - 1$.
- An ensemble of conformations will be produced by using different initial conformations.

Optimization: Gradient Descent



Gradient Descent

$$x^{t+1} = x^t + d^t$$

$$d^t = -\eta \frac{\partial f}{\partial x^t}$$

An Example - distance

- Probability of distance obeys normal distribution. $-\log(P)$
- Square of distance error = $f = (\text{sqrt}((x_1 - x_2)^2 + (y_1 - y_2)^2 + (z_1 - z_2)^2) - d_0)^2$
- $\frac{\partial f}{\partial x_1}, \frac{\partial f}{\partial y_1}, \frac{\partial f}{\partial z_1}, \frac{\partial f}{\partial x_2}, \frac{\partial f}{\partial y_2}, \frac{\partial f}{\partial z_2}$
- Partial derivative of angles is more complicated.

Gradient Descent

- **Random Initialization:** $(x_1^0, y_1^0, z_1^0), (x_2^0, y_2^0, z_2^0), \dots, (x_N^0, y_N^0, z_N^0)$
- **Update:**

$$\mathbf{X}_1^{t+1} = \mathbf{X}_1^t - \eta^* \Delta \mathbf{X} \quad \mathbf{Y}_1^{t+1} = \mathbf{Y}_1^t - \eta^* \Delta \mathbf{Y} \quad \mathbf{Z}_1^{t+1} = \mathbf{Z}_1^t - \eta^* \Delta \mathbf{Z}$$

$$\mathbf{X}_2^{t+1} = \mathbf{X}_2^t - \eta^* \Delta \mathbf{X} \quad \mathbf{Y}_2^{t+1} = \mathbf{Y}_2^t - \eta^* \Delta \mathbf{Y} \quad \mathbf{Z}_2^{t+1} = \mathbf{Z}_2^t - \eta^* \Delta \mathbf{Z}$$

•
•
•

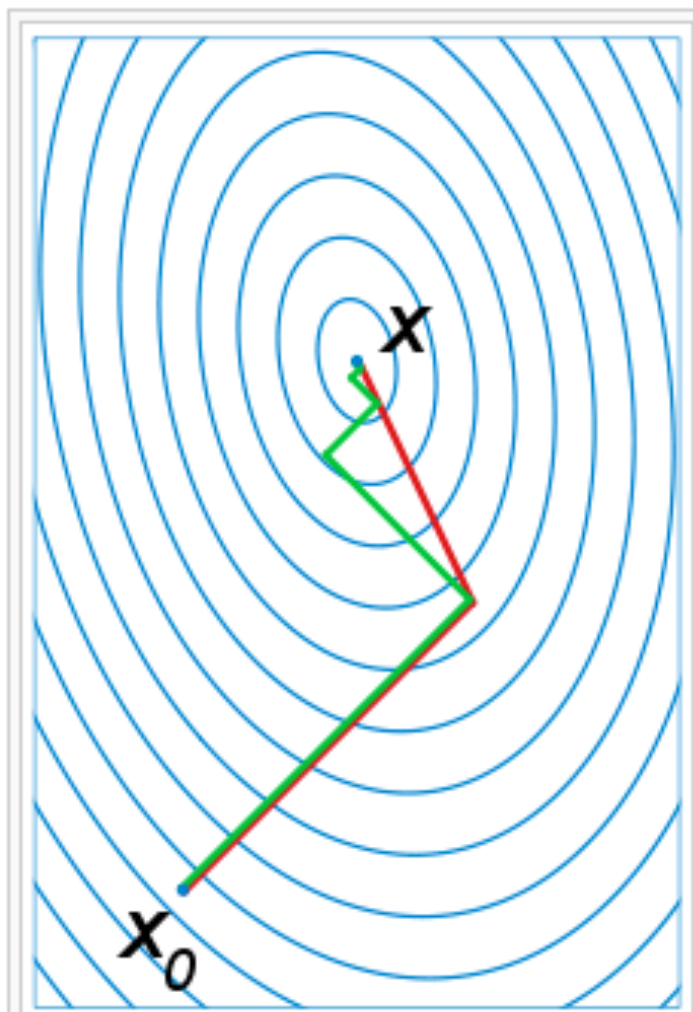
$$\mathbf{X}_N^{t+1} = \mathbf{X}_N^t - \eta^* \Delta \mathbf{X} \quad \mathbf{Y}_N^{t+1} = \mathbf{Y}_N^t - \eta^* \Delta \mathbf{Y} \quad \mathbf{Z}_N^{t+1} = \mathbf{Z}_N^t - \eta^* \Delta \mathbf{Z}$$

Conjugate Gradient Descent

$$x^{t+1} = x^t + \eta d^t$$

$$d^t = -\frac{\partial f^t}{\partial x^t} + d^{t-1}$$

$$d^t = -\frac{\partial f^t}{\partial x^t}$$



A comparison of the convergence of [gradient descent](#) with optimal step size (in green) and conjugate vector (in red) for minimizing a quadratic function associated with a given linear system. Conjugate gradient, assuming exact arithmetic, converges in at most n steps where n is the size of the matrix of the system (here $n=2$).

Spatial restraints used to model trypsin

| Type | Basis pdfs ^a | Feature pdfs ^b | Violations ^c | r.m.s. ^d | r.m.s. ^e |
|---|-------------------------|---------------------------|-------------------------|---------------------|---------------------|
| Bond lengths | 1659 | 1659 | 0 (0.1 Å) | 0.005 Å | 0.005 Å |
| Bond angles | 2250 | 2250 | 5 (10°) | 2.00° | 2.00° |
| Dihedral angles ^f | 919 | 919 | 1 (20°) | 3.40° | 3.40° |
| van der Waals contacts ^g | 531 | 531 | 0 (0.2 Å) | 0.02 Å | 0.02 Å |
| C ^α -C ^β distances | 23,538 | 11,914 | 26 (1.5 Å) | 0.22 Å | 0.47 Å |
| Main-chain N-O distances | 7480 | 3832 | 19 (1.5 Å) | 0.31 Å | 0.51 Å |
| Main-chain Φ dihedral angles | 1110 | 222 | 2 (20°) | 10.8° | 21.2° |
| Main-chain Ψ dihedral angles | 1332 | 222 | 9 (20°) | 10.6° | 20.3° |
| Side-chain χ ₁ dihedral angles | 528 | 176 | 5 (25°) | 8.4° | 16.8° |
| Side-chain χ ₂ dihedral angles | 264 | 103 | 3 (25°) | 10.2° | 13.0° |
| Side-chain χ ₃ dihedral angles | 92 | 32 | 2 (25°) | 11.9° | 48.1° |
| Side-chain χ ₄ dihedral angles | 48 | 16 | 0 (25°) | 4.5° | 21.9° |
| Disulphide bridge bonds | 6 | 6 | 0 (0.1°) | 0.007 Å | 0.007 Å |
| Disulphide bridge angles | 12 | 12 | 0 (10°) | 3.7° | 3.7° |
| Disulphide bridge dihedral angles | 6 | 12 | 0 (20°) | 10.0° | 12.9° |
| <i>cis</i> -Peptides ^h | 0 | 0 | | | |

Group Formation

- **Group 1:**
- **Group 2:**
- **Group 3:**
- **Group 4:**

Project 1

- Design and develop a template-based protein structure modeling tool
- Assess its performance on a few TBM targets used in CASP12 or CASP13 benchmark
- Reference programs: (see later slides)

Project Directory

- Project1
- ---- src: source code
- ---- bin: binary
- ---- lib: library
- ---- data: data
- ---- training: training
- ---- test: test cases
- ---- doc: document / references / presentation / report
- ---- other: third-party programs

Discussion of Your Project Plan

- Data preparation & data sharing (cloud computing)
- Algorithm development (initialization, restraints extraction & representation, sampling, optimization): creative, alternative, plural
- Implementation: interface, design, platform, languages, code base / from scratch, task assignment, timeline, progress track
- Evaluation plan (metrics, tools, data, objective, comprehensive, expectation)
- Challenges, Technical Hurdles, Feasibility, Strength, weakness, Risks
- Visualization
- Software Package (installation, test cases)

Useful Tools

- Loop modeling: <http://www.math.unm.edu/~vageli/codes/codes.html>
- Tools convert between (x,y,z) coordinates and (phi, psi) angles: a Rosetta function. Rosetta can also create model loops.
- ModLoop a web server for loop modeling based on Modeller
- Add side chains to main chain – SCWRL
- An open source template-based modeling tool - MTMG

Modeller

- <https://salilab.org/modeller/>
- A widely used, well-documented template-based modeling tool

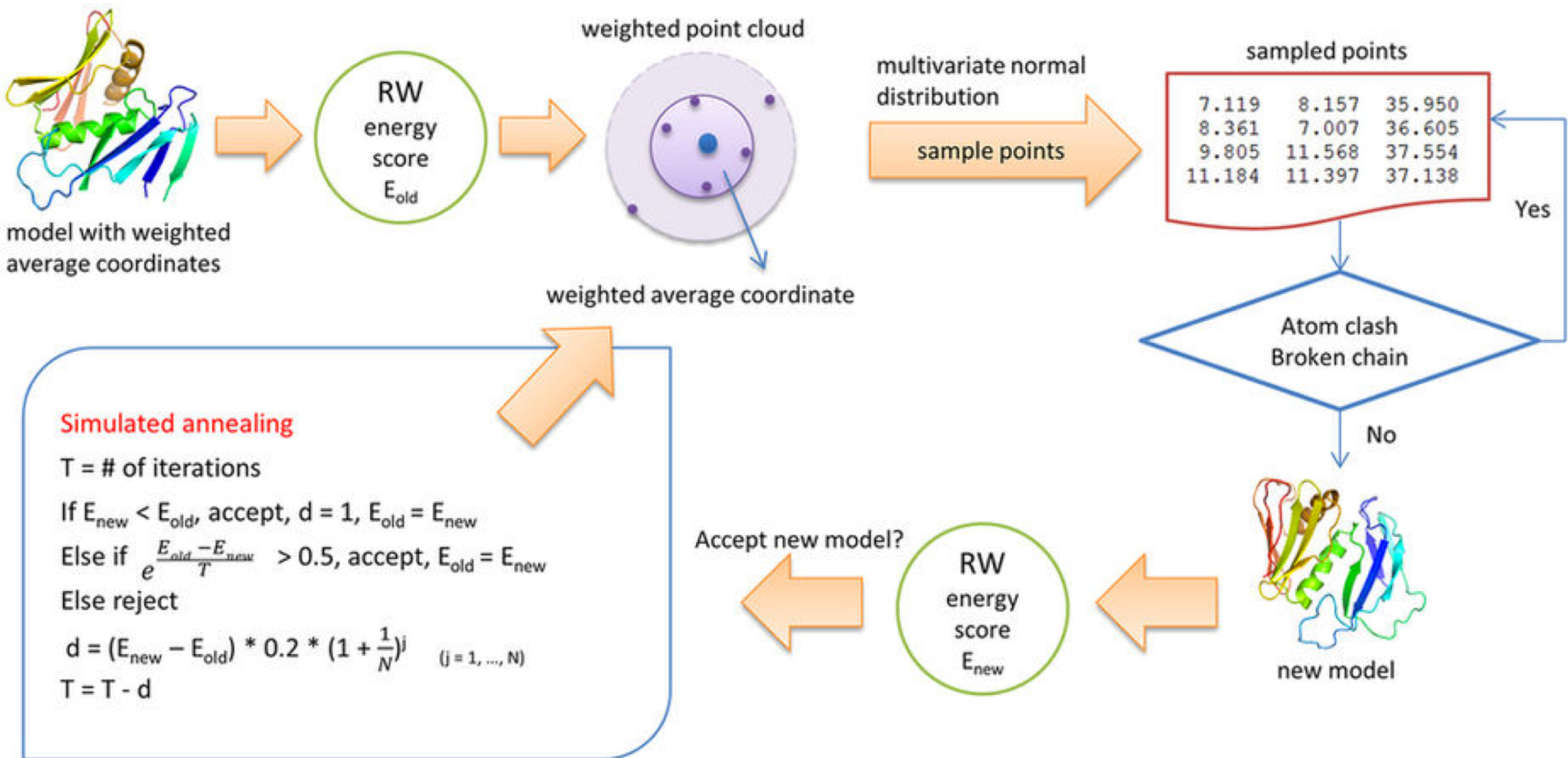
Integrative Modeling Platform

- IMP: <https://integrativemodeling.org>
- It implements all kinds of optimization methods including gradient descent. (you may refer to some source code there)

MTMG

- A stochastic point cloud sampling method for template-based protein comparative modeling. Scientific Reports, 2016.
- Source code is available:
http://sysbio.rnet.missouri.edu/multicom_to_olbox/tools.html

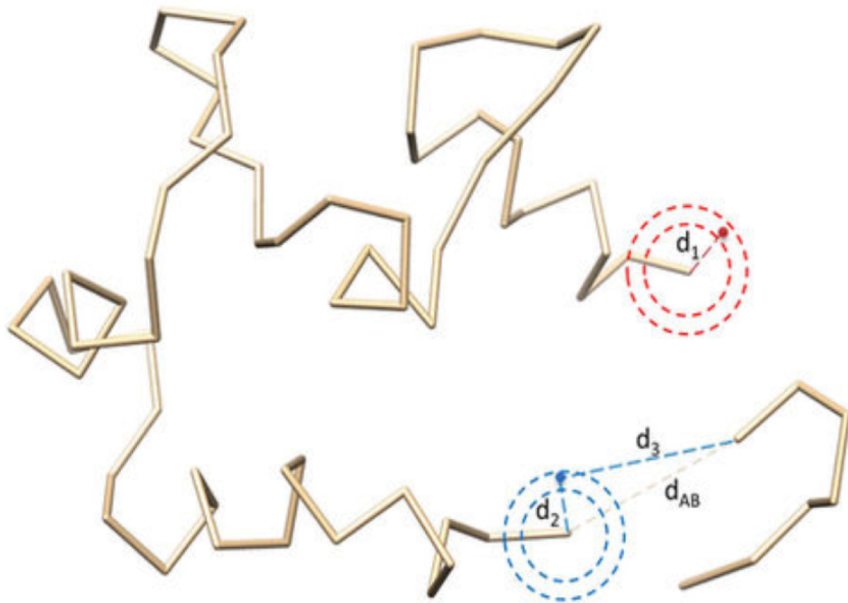
Workflow of MTMG



Can model unaligned loops

Handle Gaps

d

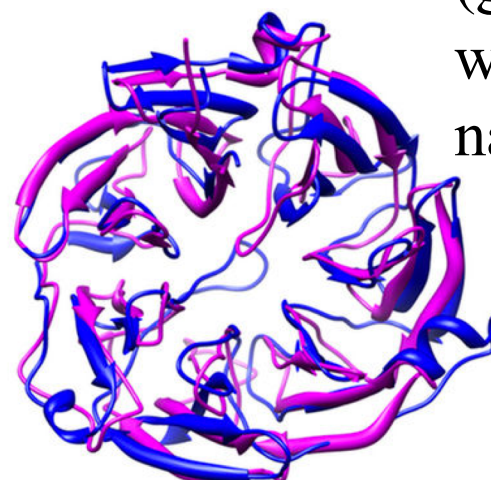
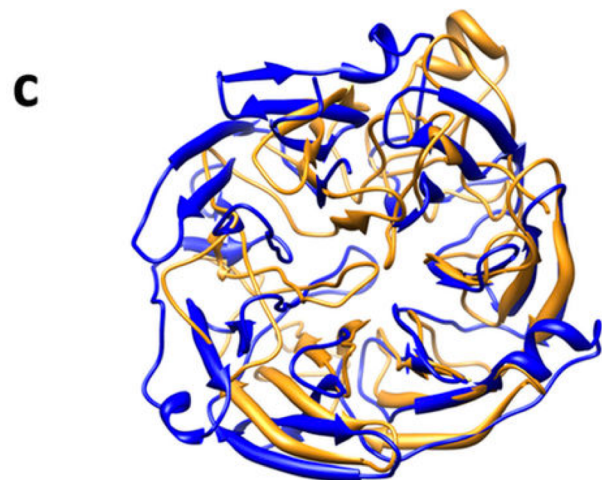
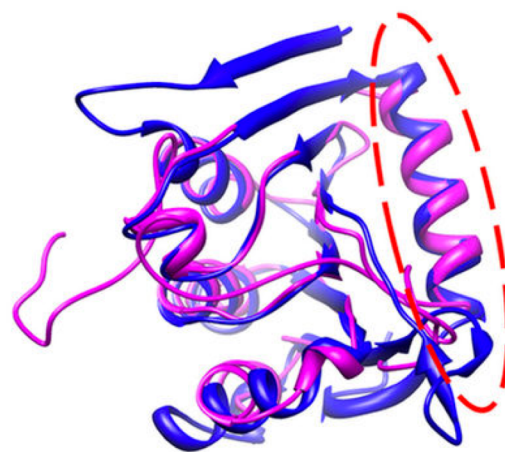
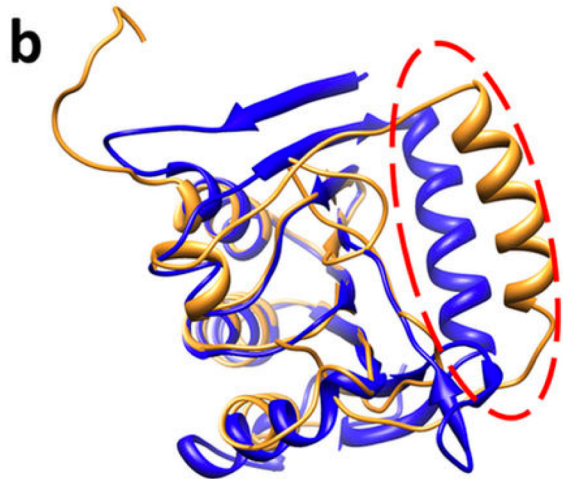
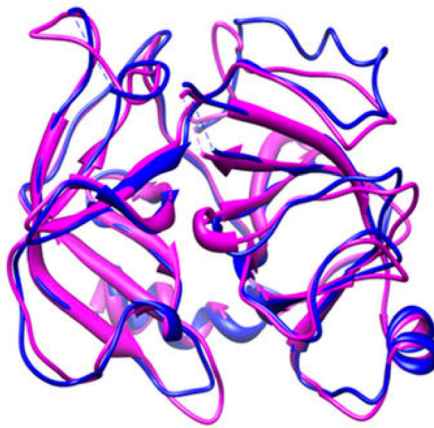
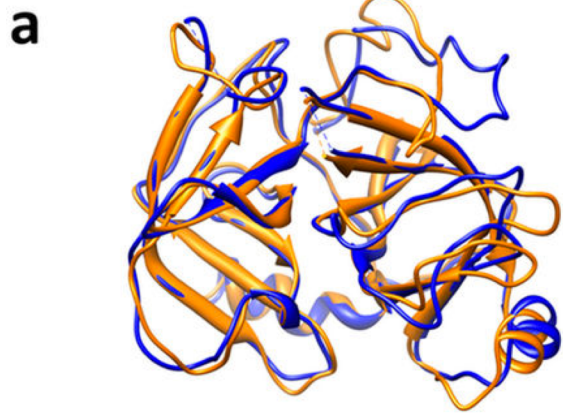


Sampling points for gaps. The radius of the outside circle is 4.5 Å, and the radius of the inner circle is 3.5 Å.

The sampling algorithm randomly samples point between the two circles. In the region circled by red, the gap is at the N-terminal.

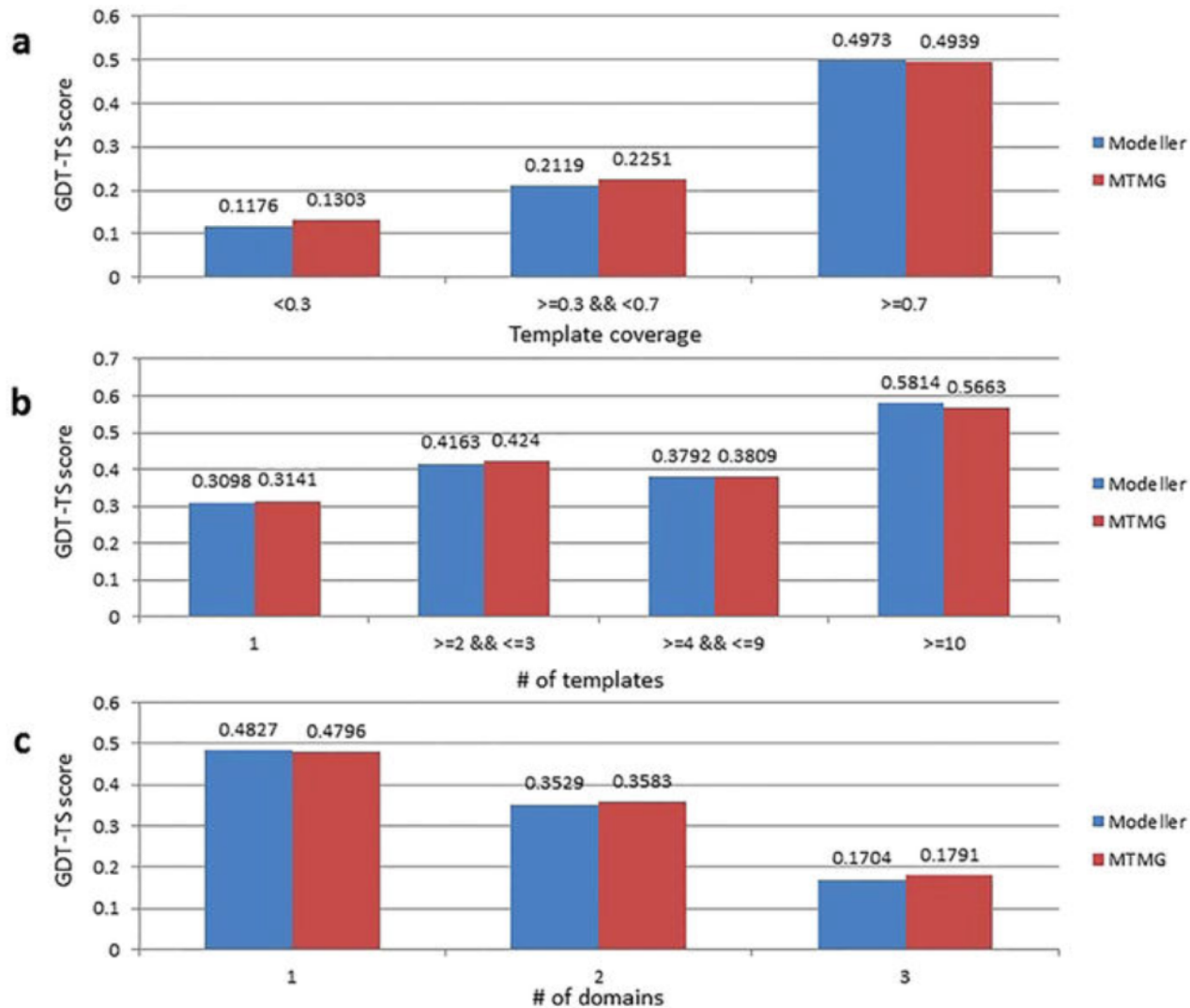
The distance d_1 between an accepted sampled point and the first covered residue is between 3.5 Å and 4.5 Å.

In the region circled by blue, the three-residue gap is in the middle, and the distance between the two ends of the gap (d_{AB}) is 8.2 Å. The distance d_2 between an accepted sampled point and the last covered residue before the gap is between 3.5 Å and 4.5 Å. The distance d_3 between an accepted sampled point and the first covered residue after the gap is between 4.1 Å and 11.4 Å.



Three examples illustrating (a) the successful template weighting and combination, (b) the successful template superposition, and (c) the successful domain division and combination of our method. The models predicted by Modeller (gold) and MTMG (purple) were superposed with the native structure (blue).

Figure 5: Comparison of GDT-TS score between the MTMG models and the Modeller models from three aspects on CASP11 targets.



(a) MTMG performed better than Modeller on targets with <math><0.7</math> template coverage. **(b)** MTMG performs better than Modeller on targets covered by <math><10</math> templates. **(c)** MTMG performs better than Modeller on targets containing multiple domains.

Key Milestones of Project 1

- Class discussion on Feb. 20
- Presentation of your plan on Feb. 25
- Presentation of your results on Mar. 6