2D and 3D Genome Structure Modeling

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Genome – Code of Life



СТ	С	С	G	G	А	С	А	А	А	т	С	G	А	т	G	G	С	т	т	т	С	G
AA	т	C	С	G	Т	С	G	т	т	Т	Т	Т	т	А	т	G	С	С	т	Т	Т	А
AG	G	A	G	A	А	G	С	т	A	т	G	C	G	т	G	A	т	G	С	С	G	т
AT	т	С	G	С	G	т	C	С	A	т	G	A	т	Ċ	C	G	G	С	G	С	С	G
AT	С	G	С	Т	С	C	A	C	A	т	C	A	A	С	А	A	A	A	C	т	A	т
GG	т	A	A	G	A	A	т	G	A	G	G	C	A	A	т	т	G	т	А	т	A	G
GC	А	G	A	т	G	т	G	C	C	C	G	A	G	A	т	С	G	G	G	т	G	G
CT	A	Т	A	Т	A	A	С	G	A	т	C	т	A	A	C	С	G	Т	т	G	G	G
GA	A	C	A	G	A	т	G	Т	A	Ġ	C	т	C	A	C	С	A	Т	A	C	C	т
CG	т	G	G	A	G	A	Ġ			A	Ġ	C	A	A	А	C	C	т	G	C	G	C
AA	A	G	A	G	Т	G					G	C	A	Т	С	G	C	C	C	G	A	Т
GC	G	Т	A	G	Т							C	A	A	A	G	G	G	G	A	G	G
GT	G	Т	G	A	G							т	т	A	A	A	G	A	C	G	C	A
ΤA	А	G	С	т	т	G	A				C	A	A	т	А	G	т	т	А	A	т	т
CG	С	т	G	A	C	G	С	C	C	A	т	A	A	G	G	C	G	A	G	G	G	G
AC	G	C	C	Т	G	A	G	C	G	A	A	т	C	Т	A	A	т	G	G	A	т	G
AT	т	G	C	т	A	G	G	G	C	Т	G	G	G	A	т	Т	C	A	C	Т	т	C
AT	С	G	Т	Т	Т	A	Т	C	C	A	С	A	С	С	C	A	A	G	C	G	A	A



Genome Sequencing (1D)





The Genomic Era

Collins, Venter, Human Genome, 2000











Personal Genome

Sequencing Revolution













\$1000 Personal Genome!

http://www.futuretimeline.net/blog/2014/01/16.htm#.U3Vg-FhdWzs

3D Shape



http://images.google.edu

Genome





までのする中からものながものでのなものなかでものとれたとものであっていたのでのなかなるかでもあたのなのでものできる CGGCCCATGGCTCCTCCACCTAACCAGCAGTATGGACAGCAATATGGTCAGCAATATGA CAGCAGGAACAGGCAAAAGGCACAATTAAGCAACGGCTACAACCAATCCTAATGTAAAC TCCAATAT97AC99FCCACCCCAGAATAT97CATTACCTCCACCTCAAACACAAAC7AT CAAGGTACAGACCAACCTTATCAGTATTCTCAATGTACTGGGCGTAGAAAGGC ATCSGTATAAACTACATAGGTTCAAAAAATCAACTGCGTGGTTGTATCAATGATGCTCAT AACAPCTTCAACTTTTTGAACTAAFGGGTACGGTTACAGTTCAGAFGACAFTGTCATATAT LCTGATGATCAGAACGATTTGGTCAGGGTTCCCACTAGGGCTAATATGA CAATGGTTGGTCAAGGATGCGCAACCCAATGATTCTTGGTTCCTTCATTATTC GOPOSCCAAACPGAAGATTTGGAFSGGGGGGGGAGGATGGGATGGGATGGATGTTATATAT COGGTCGATTTOGAAACTCAAGGGCCAATTATOGACGATGAAATGCACGATAT. AAGCCCTTACAACAAGGTGTTAGACTAACAGCATTGTTTGACTCTTGTCATTCGGGTACA GTGTTSGATCTTCCATATACC7ATTCTACTAAGGGGTATTATTAAGGAGCCCAATATTTGG AAGGATGTTGGCCAAGATGGCCTGCAAGCAGCTATTTCATATGCCACAGGAAACAG GCTTTSATTGSTTCTTTAGGTTCTATATTCAAGACCGTTAAGGGAGGTATGGGCAATAA GGTTCGAABGATAATCAAACTTCTGCAGATGCTGTCGAAGATGGGCAAAATACAGGTGCA ATGTCCCACGCCTTCATCAAGGTTATSACTTTACAACCACAGCAATCATATTTATCTCTT TTACAGAACATGAGGAAAGAATTGGCTGGTAAGTATTCTCAAAAAACCACAATTATCATCG TCACACCCTATTGACGTAAATCTGCAATTTATTATGTAG



>95% non-coding regions of a genome are not junk!!

Genome Conformation





ACAACAACGCTGGTGGTAATAATGGCTACCAA ASTATSGACASCAATATSGTCASCAATATSAA AAAATGATCAGCAATTCAGTCAGCAATATGCT ATAACAGGCCTGTGTGTATCOCCCCCCCCAATTC **SCAACSGCTACAACAATCCTAATGTAAACGCA** POPCATTACCTCCACCTCAAACACAAACTAT TTCAATGTACTGGGCGTAGAAAGGCTTTGATT **NTCAACTGCGTGGTTGTATCAATGATGCTCAT** accostracactecacatesacatetorcatatea PTCCCACTAGGGCTAATATGATTAGGGCCATG **NTGATTCTTTGTTCCTTCATTATTCTGGACAT** ACGAAGAAGATGGGATGGATGATGTTATATAT **TTATOGAOGATGAAATGCAOGATATAATGGTG** CAGCATTOTTGACTCTTGTCATTCGGGGTACA CTAA0607ATTATTAA06A6CCCAATATTT00 CAGCTATTTCATATGCCACAGGAAACAGGGCT TCAAGACCGTTAAG96A9G7A7699CAA7AAT AATTOTCAGCAGCAGATGTTGTTATCA ATGCTGTCGAAGATGGGCAAAATACAGGTGCA CTTTACAACCACAGCAATCATATTTATCTCTT **STAAGTATTCTCAAAAACCACAATTATCATCS** PTATTATGTAG

Liberman-Aiden et al., 2009

3D Genome Structure is Important



Multi-Level Chromosome Structure



DNA double helix

DNA is further packaged. **Nucleosomes** are arranged together into **a fiber** approximately 30 nanometers in diameter. The *precise structure of the chromatin fiber is not known*. Chromatin fiber is further organized into **chromatin loops**, and chromatin loops are further organized into higher-order structures. It has been suggested that **packaging plays a role in gene expression** (gene expression may require associated DNA to open up and acquire an unpackaged conformation). The fully condensed chromosome structure is only seen during mitosis.

Model 1 (Riken)



The DNA is a remarkable molecule in many ways. It encodes our entire genome, and if stretched out in a thin thread would measure **1.8 m** in length.

http://www.rikenresearch.riken.jp/eng/frontline/6485

Size of Elements



NM: 10⁻⁹ meter

A complex of DNA and basic proteins (such as **histone**) in eukaryotic cells that is condensed into chromosomes in mitosis and meiosis.

There are two types. **Heterochromatic** is densely-coiled chromatin that appears as nodules in or along chromosomes and contains relatively few genes. **Euchromatic** is the lesscoiled and genetically active portion of chromatin that is largely composed of genes.

Size of Elements



Chromosomes



http://www.copernicusproject.ucr.edu/ssi/HSB iologyResources.htm

Two Compartments

Linear chromosome: Active genes: orange Inactive genes: blue



Chromatin looping between active genes and regulatory elements and clustering of genes at the site of active transcription facilitates formation of chromatin globules.

Active gene cluster associate with other expressed genes in active neighborhoods while inactive genes cluster in silent neighborhoods.

Active and silent neighborhoods associate in cis and in trans to form larger active and inactive compartments.

Nuclear organization reflects clustering of active and inactive loci in distinct compartments forming a fractal globule.

Current Opinion in Cell Biology

A. Sanyal et al., Current Opinion in Cell Biology, 2011

Chromosome Conformation Capturing Techniques

Chromosome Conformation Capturing (Hi-C)



Hi-C Protocol

- Cells are cross-linked with formaldehyde
- DNA is digested with a restriction enzyme and ligated, resulting enriched with cross-linked elements with a biotin marked at the junction
- Shearing DNA and selecting biotin-containing fragments to create a Hi-C library
- Sequence the library to create a catalog of interacting fragments

Genomic Spatial Interaction (Contact) Data



ATGTATCCAGGTAGTGGA TOOTOOTAATAATOOCTAOCAA CEGCCCATEGCTCCTC CCTAACCAGCAGTATGGAC GCAA7A7GG7CAGCAA7A7GAA CAGCAGTATOGACAGO CAAPTCAGTCAGCAAPAPGC CAGCAGGAACAG ACTGATGATCAGAACGATTTGGTCAGGGTTCCCACTAGGGCTAAT GATTAGOODCATO CANTGGTTGGTCANGGATGCGCAACCC GGTGGCCLALCTGALGLTTTGGA COGGECGATTTOGALACTCAAGGGCCAATTATOGAC AAGCCCTTACAACAAGGTGTTAGACTAACAGC OTOTTOGATCTTCCATATACC7ATTCTACTAA00007AT AAGGATGTTGGCCAAGATGGCCTGCAAGCAGCTATTCATATGCCACAGGA GTOGATAGAGAACGCGTGAGACAGATCAAATTC GETTOGALGGATAATCAAACTTCTGCAGATGCTGTOGAAGATGGGG ATGTCCCACGCCTTCATCAAGGTTATSACTTTACAACCACAGCAATC TTACASAACATGAGGAAAGAATTGSCTGSTAAGTATTCTCAAAAACCACAATTATCATCS TCACACOCTATTGACGTAAATCTGCAAT

Map reads to the human genome sequence



C[i,j] = # contacts

1

2

n

Intra- / inter-chromosome contact map

Wang et al., 2013



Proximity Matrices

2D Chromosome Contact Map



Chromosome Conformation Capturing

Construct 3D Shape of Genome





Images.google.com

Data Set I

- A normal human lymphoblastoid cell line (Bcell)
- 8.4 million read pairs uniquely mapped to the human genome reference sequence
- 6.7 million corresponded to long-range contacts between segments > 20 kb apart

Liberman-Aiden et al., 2009

Genome Wide Contact Map

- Divide genome into 1-Mb regions (loci)
- M_{ij}: number of contacts between loci i and j
- The matrix reflects an ensemble average of the interactions in the original sample of cells
- Represented as a heat map



(B) Hi-C produces a genome-wide contact matrix. The submatrix shown here corresponds to **intrachromosomal interactions on chromosome 14**. (Chromosome 14 is acrocentric; the short arm is not shown.) Each pixel represents all interactions between a 1-Mb locus and another 1-Mb locus; intensity corresponds to the total number of reads (0 to 50). Tick marks appear every 10 Mb. (C) We compared the original experiment with results from a biological repeat using the same restriction enzyme [(C), range from 0 to 50 reads]. Correlation is 0.99.

Relation between Euclidean Distance and Genomic Distance

- Average intrachromosomal contact probability
 I_n(s) for pairs of loci separated by a genomic distance s on chromosome n.
- I_n(s) decreases monotonically on every chromosome
- Even at distances > 200 Mb, I_n(s) is always much greater than the average contact probability between different chromosomes



Implication: Chromosome territory

Probability of contact decreases as a function of genomic distance on chromosome 1, eventually reaching a plateau at ~90 Mb (blue). The level of interchromosomal contact (black dashes) differs for different pairs of chromosomes; loci on chromosome 1 are most likely to interact with loci on chromosome 10 (green dashes) and least likely to interact with loci on chromosome 21 (red dashes). Interchromosomal interactions are depleted relative to intrachromosomal interactions.



Observed/expected number of interchromosomal contacts

between all pairs of chromosomes. Red indicates enrichment, and blue indicates depletion (range from 0.5 to 2). Small, generich chromosomes tend to interact more with one another, suggesting that they cluster together in the nucleus.

Human chromosomes

expected number of contacts between chromosome i and j was calculated by:

$$E_{i,j} = R_i \times R_j \times N_{INTER},$$

where R_i and R_j are the fractions of inter-chromosomal reads associated with *i* and *j*, respectively, and N_{INTER} is the total number of inter-chromosomal reads for a cell sample. The actual observed number of inter-chromosomal contacts between chromosomes *i* and *j* divided by the expected number $E_{i,j}$ indicates the enrichment or depletion of inter-chromosomal contacts between them.

Normalizing Contact Map by Expected Number of Contacts at Genomic Distance



Dividing each entry in the contact matrix (M) by the genome-wide average contact probability for loci at that genomic distance. The normalized matrix shows many large blocks of enriched and depleted interactions, generating a plaid pattern

Pearson Correlation Map



If two loci (here 1-Mb regions) are nearby in space, we reasoned that they will share neighbors and have correlated interaction profiles.

This process dramatically **sharpened the plaid pattern**; 71% of the resulting matrix entries represent statistically significant correlations ($P \le 0.05$).

The **plaid pattern** suggests that each chromosome can be decomposed into two sets of loci (arbitrarily labeled A and B) such that contacts within each set are enriched and contacts between sets are depleted.

Principle Component Analysis



The first two principal components (PC) clearly corresponded to the plaid pattern (positive values defining one set, negative values the other).

The entire genome can be partitioned into two spatial compartments such that greater interaction occurs within each compartment rather than across compartments.

FISH Validation of Two Compartments





L1 – L3: Compartment A L2 – L 4: Compartment B





Contacts and Physical Distance Measured by FISH

- A strong correlation was observed between the number of Hi-C reads m_{ij} and the 3D distance between locus i and locus j as measured by FISH [Spearman's r = -0.916, P = 0.00003], suggesting that Hi-C read count may serve as a proxy for distance.
- Pairs of loci in compartment B showed a consistently higher interaction frequency at a given genomic distance than pairs of loci in compartment A. This suggests that compartment B is more densely packed.

Open More Accessible, **Gene Rich** Compartment **VS** less Accessible

H3K27/H3K36: activating/repressive chromatin Marks DNAsel: deoxyribonuclease I, sensitivity, measure chromatin accessibility



Contact Probability VS Genomic Distance (Power Law Distribution)



Contact probability as a function of genomic distance averaged across the genome (blue) shows a power law scaling between 500 kb and 7 Mb (shaded region) with a slope of -1.08 (fit shown in cyan).

When plotted on log-log axes, **I(s)** exhibits a prominent power law scaling between ~500 kb and ~7 Mb, where contact probability scales as s⁻¹. This range corresponds to the known size of open and closed chromatin domains.
Genome 3D Model

- **Power-law** dependencies can arise from polymer like behavior.
- Equilibrium globule: a compact, densely knotted configuration originally used to describe a polymer in a poor solvent at equilibrium
- Fractal Model: This highly compact state is formed by an unentangled polymer when it crumples into a series of small globules in a "beads-on-a-string" configuration. These beads serve as monomers in subsequent rounds of spontaneous crumpling until only a single globule of globules-of-globules remains.

Fractal Model

- Lack knots and would facilitate unfolding and refolding, for example, during gene activation, gene repression, or the cell cycle.
- In a fractal globule, contiguous regions of the genome tend to form spatial sectors whose size corresponds to the length of the original region.
- In contrast, an equilibrium globule is highly knotted and lacks such sectors; instead, linear and spatial positions are largely decorrelated

Comparison of Two Models

FOLDED POLYMER





Consistency Checking

- The equilibrium globule model predicts that contact probability will scale as s^{-3/2}, which we do not observe in our data.
- We analytically derived the contact probability for a fractal globule and found that it decays as s⁻¹; this corresponds closely with the prominent scaling we observed (s^{-1.08}).
- 3D distance between pairs of loci: s^{1/2} for an equilibrium globule, s^{1/3} for a fractal globule. Although 3D distance is not directly measured by Hi-C, we note that a recent paper using 3D-FISH reported an s^{1/3} scaling for genomic distances between 500 kb and 2 Mb

MCMC Simulation Validation

- Monte Carlo simulations to construct ensembles of fractal globules and equilibrium globules (500 each).
- Contact probability (for fractal globules, s⁻¹, and for equilibrium globules, s^{-3/2})
- 3D distance (for fractal globules s^{1/3}, for equilibrium globules s^{1/2})
- Lack of entanglements and the formation of spatial sectors within a fractal globule.





Hi-C Data Analysis II

Z. Wang, R. Cao, K. Taylor, A. Briley, C. Caldwell,
J. Cheng. The Properties of Genome
Conformation and Spatial Gene Interaction and
Regulation Networks of Normal and Malignant
Human Cell Types. PLoS ONE. 2013

Data Sets

- Primary human acute lymphoblastic leukemia (B-ALL) B-cell
- The MHH-CALL-4 B-ALL cell line (CALL4)
- The follicular lymphoma cell-line (RL)
- Sequenced by Illumina HiSeq 2000

Number of Reads of the samples

Samples	Total number of reads	Utilized for analysis
Normal B cell	12,887,282	YES
RL1	60,272,006	NO
RL2	61,043,078	NO
RL3	65,579,872	NO
RL4	125,256,746	YES
Call4_1	62,741,712	NO
Call4_2	62,607,906	NO
Call4_3	133,542,778	YES
ALL B-Cell	77,888,742	YES

Read coverage

	Read coverage of gene region	Read coverage of non-gene region	Read length
Call4 cell line	2.81129121903121	2.35780895	100
RL cell line	1.47413416423764	1.14648699	100
Normal B-cell	0.186290512630489	0.1725446	76
ALL B-cell	1.788587532589	1.49037874	120



Quality Scores for Solexa/s_7_2_sequence.txt (1st and 91st percentiles, 2nd and 3rd quartiles, and median, shown per position)



Mapping Reads to Human Genome



Un-normalized intrachromosomal heat maps for primary ALL B-Cell











Chromosome 2

Chromosome 3

Chromosome 4

Chromosome 5











Chromosome 9

Chromosome 10





Chromosome 15

Chromosome 11

Chromosome 16



Chromosome 17



Chromosome 18











Chromosome 22



Chromosome X





Chromosome 20











Chromosome 13

chromosomal heat maps for primary **ALL B-Cell**

Sequential Component Normalization: M[i,j] / |M[i]|

Repeat until symmetric











Chromosome 1

Chromosome 2

Chromosome 3

Chromosome 4

Chromosome 5











Chromosome 9

Chromosome 10







M[i,j] / |M[j]|



Chromosome 11

Chromosome 16



Chromosome 12

Chromosome 17



Chromosome 13

Chromosome 18





Chromosome 19 Chromosome 20





Chromosome 21

Chromosome 22



Chromosome X



Contact Correlation Between Cell Types



Correlate intra-contact numbers of 23 pairs of chromosomes

Inter-Chromosome Contacts and Chromosome Translocation



Cancer Causing Chromosome Translocation



- Reconstruction of translocated chromosomes
- Two cancer related genes

Comparison of Inter-Chromosome Contact Profiles of Different Cells



Gene-Gene Contact Map of HoxA Gene Cluster: HoxA gene region (27,104,502 -27,212,501) on chromosome 7,

Transcription factor controlling embrynoic development









Hi-C Databases

• 4DN data portal: <u>https://data.4dnucleome.org</u>

 ENCODE database: <u>https://www.encodeproject.org</u>

3D Genome Structure Modeling



Trieu, Cheng, 2014

Spatial Representation of Chromsome or Genome

- Divided into N equal-size (e.g. 1MB) consecutive units sequentially
- The center of a unit is denoted by a point and its coordinate (x, y, z)

Contact Driven Structure Modeling



Normalized Contact Map

Trieu, Cheng, 2014

Opportunities

- Chromosome contact data can be generated easily and cheaply
- Chromosome contact data is rather reliable
- A 3D model of a genome is very valuable in studying spatial regulation of gene expression and methylation

Challenges

- Genome and chromosome is very large (3 billion nucleotide of human genome)
- Genome structure is very dynamic
- No known experimental genome structure other than some point distance data generated by FISH
- Relationship between contact and distance is not deterministic
- Hi-C data is noisy

Maximum Likelihood or Distance-Based Approaches

- Convert interaction frequency (contact number) into distance
 - or $IF \propto 1/d^a$

 $d \propto 1 / IF^a$

• Translate distance into (x, y, z) coordinates

A MCMC Approach

M. Rousseau, J. Fraser, M.A. Ferraiuolo, J. Dostie, M. Blanchette. *Three-dimensional modeling of chromatin structure from interaction frequency data using <u>Markov chain Monte Carlo</u> <u>sampling</u>. BMC Bioinformatics, 2011.*

MCMC5C

- Formulate a probabilistic model linking 5C/Hi-C data to physical distances
- Markov chain Monte Carlo (MCMC) approach called MCMC5C to generate a representative sample from the posterior distribution over structures from IF data.

MCMC5C

- Structural properties (base looping, condensation, and local density) were defined in the models
- Applied these methods to a biological model of human myelomonocyte cellular differentiation and identified distinct chromatin conformation signatures corresponding to each of the cellular states.
- run on Hi-C data and produce a model of human chromosome 14 at 1Mb resolution that is consistent with previously observed structural properties as measured by 3D-FISH.

Other Existing Methods

 5C3D (Fraser et al.): translates IF values into physical distance estimates and then uses a gradient descent approach to find the 3D conformations.

Other Existing Methods

 Bau et al. Interactions are modeled with springs whose equilibrium length depends on the observed IF values, subject to certain constraints based on the structure of the 30-nm fiber, optimized by Integrative Modeling Platform.

Other Existing Methods

 Duan et al., convert interaction frequencies to Euclidean distances and then seek conformation minimizing the misfit, with addition of a set of clash avoidance constraints and a few prior known knowledge about the yeast genome organization. The constrained optimization problem is solved to find the best structure.

Possible Drawbacks of Existing Methods

- Objective function (sum of square difference between predicted and derived distance) is debatable.
- Assume each IF is equally reliable.
- The absence of an underlying probabilistic model, preventing the calculation of confidence intervals on specific structural properties (e.g. distance between two genomic sites)

Probabilistic Model of Chromatin Conformation

- A chromosome is modeled as a continuous piece-wise linear curve in 3D.
- Theoretical interaction frequency between fragment i an j, denoted IF(i, j), is inversely correlated with the distance between two fragments in 3D conformation: IF(i,j) = f(D_s(i,j)), where D_s(i,j) is the Euclidean distance between sites i and j and f is an appropriately chosen function.

$$f(D_{\mathbf{S}}(i,j)) \propto 1/D_{\mathbf{S}}(i,j)^{\alpha}$$

Probabilistic Model of Observed IF and Theoretical IF

$\widehat{IF}(i,j)|IF(i,j),\sigma(i,j)] =$ $N(\widehat{IF}(i,j);IF(i,j),\sigma(i,j)^2$

re *N* (*x*; μ , σ^2) is the normal density functic

Observed IF and Theoretical IF (Hi-C)

$$\Pr[\hat{r}(i,j) | r(i,j)] = N(\hat{r}(i,j); r(i,j), r(i,j) + \kappa).$$
(2)

The role of κ , which we set to 10, is to avoid having small read counts being assigned too low a variance.

Posterior Probability (Structure | IF data)

The observed data \widehat{IF} defines a posterior distribution over the set of possible conformations of the chromatin: $\Pr[\mathbf{S}|\widehat{IF}] = \Pr[\widehat{IF}|\mathbf{S}] \cdot \Pr[\mathbf{S}] / \Pr[\widehat{IF}]$. Since there are no constraints imposed on the structure space and the probability of the observed data (\widehat{IF}) is constant with respect to \mathbf{S} , we get $\Pr[\mathbf{S}|\widehat{IF}] = \zeta \cdot \Pr[\widehat{IF}|\mathbf{S}]$, for some constant ζ , and thus

$$\Pr[\mathbf{S}|\widehat{IF}] = \zeta \cdot \prod_{i,j} \Pr[\widehat{IF}(i,j)|IF(i,j) = f(D_{\mathbf{S}}(i,j),\sigma(i,j))].$$
Sampling Conformations from Posterior Distribution to maximize probability

- A random structure R₀ is initially chosen to seed the process (t=0), where each point is placed randomly in a cube of side length 10*avg(f(IF)).
- Repeat: The current structure R_t is randomly perturbed to obtain a new structure R_t. If Pr[R_t | IF]
 > Pr[R_t | IF], the perturbation is obtained and we set R_{t+1} = R_t. Otherwise, we set R_{t+1} = R_t.
- For values of t sufficiently large, find a structure with high probability: Pr[S|IF], let R_t=S.

Random Structure Perturbation

- Randomly choose one point S(i) along the structure and moving it by a vector v randomly choosing within a sphere of radius r (e.g. r = 0.25 nm)
- The likelihood of the resulting structure is then quickly obtained from that of the old by updating the terms corresponding to the pairs of points involving i.

Assessing Mixing

- R₁, ..., R_k of early iterations are highly dependent on R₀.
- Determine at what point m, the Markov process has mixed, i.e., R_m is independent of R₀
- After mixing, i.e. for k>= m, any sample R_k is representative of the target distribution. For d sufficiently large, R_k and R_{k+d} are independent.

Convergence Determination

- Run two independent chains R and R' in parallel, from independently chosen initial conformations R₀ and R_{0'}.
- Mixing is achieved if the samples {R_{k/2}, ..., R_k} and {R'_{k/2}, ..., R'_k} cannot be distinguished from each other. Specifically, the average pairwise structural distances among R_k is compared to that between R_k and R_{k'}.
- After mixing is achieved, collect samples every d=k/20 iterations.

Clustering of Structure Ensembles

- Distance metric: N*N intra-structure distance matrix Ds.
- The distance (S,T) between two structures S and T is:

$$dist(\mathbf{S},\mathbf{T}) = \sqrt{\sum_{i,j} (D_{\mathbf{S}}(i,j) - D_{\mathbf{T}}(i,j))^2}$$

Structure Clustering

- Hierarchical clustering
- Visualization: tree dendrogram
- Visual inspection is performed to determine the tree height cutoff and number of subfamilies
- Choose maximum likelihood structure from each cluster as representative and assigning it a weight proportional to the number of structures in its cluster.

Hierarchical Clustering



Convert IF to distance

 The most accurate model is the one that is best able to predict unseen pairwise interaction frequencies. For each of a set of possible a leave-one-out cross-validation was performed. Find a to minimize

$$MSE(\alpha) = \frac{1}{n} \sum_{(i,j)} (D_{\mathcal{S}^*_{(i,j);\alpha}}(i,j)^{-\alpha} - I\widehat{F(i,j)})^2.$$



C (Distance Scaling Factor) Calibration

Without physical measurement of the distance between pairs of points along the sequence, it is difficult to accurately estimate the value of C. However, based on the average IF value of pairs of fragments located less than 5kb apart along the sequence and following Bystricky et al. [51] that packed chromatin has a physical length of 1 nm for every 110-150bp, C was estimated as approximately 50 nm.

Assessment of Mixing



Figure 4 Mixing of parallel *MCMC5C* runs (HB-1119 dataset). Distance between consecutive structures (sampled every 10^6 iterations) from within one of two parallel *MCMC5C* runs (blue and red curves) or across the two runs (green curve), on the HB-1119 5C dataset. The runs converge to the same distribution very rapidly (in less than 250 seconds) and the cross-run distance (green) drops to within the same range as the within-run distances (blue and red curves) after 350×10^5 iterations.

Experiment

- Figure 4 shows that mixing is achieved after approximately 350 * 10⁵ iterations, which requires less than 250 seconds of running time. Passed this point, structures sampled every 10⁶ steps from the two parallel runs are undistinguishable from each other and sample structures from the same distribution.
- 250 structures were sampled after burn-in from each of the two runs. The two ensembles of structures were then combined and the 500 structures were clustered based on their structural similarity
- Analysis of the two THP-1 5C datasets produced similar results, and runs of a larger number of parallel MCMC chains confirm that they all sample similar structures.

Simulation Verification

Gold structure: a computationally constructed 3D structure used to generated IF data. Simulated structure: models constructed from the IF data of the gold structure. Verification by Sampling from Simulated True **Structures**



Figure 6 HB-1119 Structures from simulated data aligned to gold standard structure. The "gold standard" structure is used as a reference structure to which structures from four different parallel *MCMC5C* runs on simulated data generated from the gold standard structure are aligned. The gold standard structure is shown highlighted with a white glow and the transcription start sites for the HoxA genes are annotated. The structures found from the simulated data are shown in superimposition to the gold standard structure and show a high degree of alignment.

Structure Clustering and Sub-Structure Families. Sub-structure families may correspond to chromatin structures of cells in different stages



Figure 5 Mixing and subclustering of HB-1119 structures. Mixing and hierarchical clustering (Ward's method) of structure similarity. The five-hundred structures come from two parallel *MCMC5C* runs on the HB-1119 dataset (pools of 250 structures from each run were used). The colors along the top indicate which run each structure originated from (run one = blue, run two = red) and demonstrates that the sampling process has successfully mixed. The blocks in the heatmap and the dendrogram indicate the presence of sub-clusters of structures (numbered in the dendrogram). The two clusters (numbered 1 and 2) both contain structures from the two parallel runs (blue and red vertical bars), indicating that the structures are conserved across runs and are not an artifact of the burn-in process.

Conformations of HoxA in Undifferentiated and Differentiated Conditions



Figure 7 Models of HoxA cluster before and after differentiation. Maximum likelihood structures found by *MCMC5C* from the undifferentiated and differentiated THP-1 datasets (A and B, respectively). The HoxA gene transcription start sites are annotated on each of the structures.



Figure 8 THP-1 clustering of undifferentiated and differentiated structures. Hierarchical clustering (Ward's method) of one-thousand structures from four parallel *MCMC5C* runs, two on the undifferentiated THP-1 dataset and two on the differentiated THP-1 dataset (250 structures each). The colors along the top indicate which state each structure originated from (undifferentiated run one = blue, run two = red; differentiated run one = pink, run two = orange) and demonstrate a clear distinction between the two states, indicating that the undifferentiated and differentiated cell states specify different structure signatures.

Structural Variation and Conservation

The subset of fragments that are the most conserved across the ensemble of structures are found to lie within the central core region of the structures. These fragments are spatially close to each other and may be involved in looping contacts that are important for the maintenance of the chromatin structure and are therefore highly conserved.

On Hi-C Data (Data Set II)

Model the long arm of human chromosome 14 (88.4 Mb region) from Hi-C data published by Lieberman-Aiden et al. [18] at a 1Mb resolution (89 fragments in total). Lieberman-Aiden et al. [18] proposed the existence of two physically disjoint compartments, whereby compartment A was found to correlate with open and actively transcribed chromatin, while compartment B was found to be more densely packed and repressed.

MCMC5C Availability

 MCMC5C modeling movie: <u>https://www.youtube.com/watch?v=2aIQvU</u> <u>DIGNc</u>

Distance-based approach: convert IF to distance

- Duan et al., the resulting conversion approximately follows d $\propto 1/IF$.
- Mateos-Langerak et al . [50] also suggest a relationship of the form d \propto 1 / IF^a .
- Bau et al . [28] convert their IF via a linear transformation of the IF' s z-score.

Spatial Representation of A Genome Region at a Scale



- A genome region (e.g. a chromosome) is divided into N equal / variable size units sequentially
- The spatial position of the center of a unit is denoted by a point and its coordinate (x, y, z) and constraints on the size of unit (radius of sphere)
- The consecutive points are joined into fragments forming the folding trace of the region.

Structure Construction at One Scale

Initial Structure Representation of Units

Contact Map Between Units



J. Cheng, NSF CAREER Project Plan, 2011, 2012, 2013

A Data Driven Optimization Approach

• Convert observed interaction frequencies into distance map



α: conversion parameter (positive number)

- Objective: Adjust positions (x,y,z coordinates) of beads in 3D space to satisfy converted expected distances as well as possible
- Challenges: approximated distances, noise, conflicts

Tuan and Cheng, NAR, 2017

Problem of Traditional Objective Functions

Square Error



- Very sensitive to noisy / conflicting distances
- Cannot build 3D models of large genomes involving noisy inter-chromosomal contacts

Deriving Soft Constraints by Lorentzian Function

Use Lorentzian function to measure the satisfaction of a distance restraint



 Tolerate noisy restraints and maximize the satisfaction of feasible restraints
 Tuan and Cheng, NAR, 2017

Objective Function

- Objective function
 - Sum of all distance constraints
 - Adjacent beads have maximum weight to enforce their proximity

$$fn = \sum_{|i-j|=1} \frac{c * c * IF_{\max}}{c * c + (x_{ij} - d_{ij})^2} + \sum_{|i-j|\neq 1} \frac{c * c * IF_{ij}}{c * c + (x_{ij} - d_{ij})^2}$$

 c is set to average of d_{ij} to control gradient vanishing during optimization

Tuan and Cheng, NAR, 2017

Large-Scale Adaptive Step-Size Gradient Ascent





Tuan and Cheng, NAR, 2017

Correlation Between Reconstructed Distances and True Distances



Signal to Noise Ratio

Yeast datasets (Duan et al. Nature 2010)

3D Genome Model for Human



A Open Source Tool - LorDG

• Github: https://github.com/BDM-Lab/LorDG



3D genome reconstruction with Lorentzian objective function

🕝 7 commits	រ្ទ 1 branch	🛇 1 release	L 0 contributors		
Branch: master ▼ New pull request]		Find file Clone or download -		
💽 tuan add jar file to make contact mat	rices from raw HiC data in 2009		Latest commit f7db508 on Dec 7, 2017		
🖿 bin	run 1 thread with the main thre	ad	a year ago		
examples	initial commit		a year ago		
🖿 lib	add dependency library		a year ago		
make_input	add jar file to make contact ma	atrices from raw HiC data in 2009	4 months ago		
src	add dependency library		a year ago		
README.md	add readme file		a year ago		
paramaters_settings.txt	initial commit		a year ago		
E README.md					
3D Genome Struct	ure Modeling by Lor	entzian Obiective Fur	action		

Contact-Driven Modeling at Chromosome Scale

- **Input**: initial representation of chromosome, contact map, and physical distance restraints
- **Objective**: find 3D chromosome structures that satisfy the contact map and physical contact restraints as much as possible.
- Scoring Function
- Optimization
- **Output**: an ensemble of 3D shapes

Data Preparation

- Data Sets: Normal B-Cell, ALL B-Cell
- Unit Size: 1Mb
- Unit Number: Chr. 1, 248 –
 Chr. 22, 50
- Contact map normalization: $C_{ij}' = C_{ij} / expected IF$
- Remove noisy contacts with low interaction frequency

Normalized Interaction Frequencies (IF) on the normal B-Cell

Chromosome	Max IF	Min IF	Average IF		
1	86.34	0.035	1.35		
2	83.04	0.037	1.53		
3	59.81	0.037	1.74		
4	70.76	0.035	1.95		
5	171.92	0.040	1.84		
6	59.68	0.031	1.86		
7	130.00	0.035	1.99		
8	122.22	0.056	2.29		
9	190.85	0.043	2.86		
10	76.12	0.085	2.31		
11	58.51	0.040	2.19		
12	85.86	0.042	2.23		
13	151.09	0.212	3.62		
14	112.48	0.116	3.42		
15	103.02	0.110	3.14		
16	100.09	0.046	3.31		
17	86.08	0.081	3.12		
18	108.33	0.173	3.80		
19	96.56	0.061	4.82		
20	106.89	0.089	4.05		
21	63.01	0.174	5.98		
22	79.05	0.057	5.83		

Scoring Function for Optimization

$$S = \sum_{\substack{\text{contacts} \\ |i-j| \neq 1}} \left(tanh(d_c - d(i,j)) * \frac{IF_{ij}}{T} + W1 * \frac{tanh(d(i,j) - d_{min})}{T} \right)$$

$$+ \sum_{\substack{\text{non-contacts} \\ |i-j| \neq 1}} \left(W2 * \frac{tanh(d_{max} - d(i,j))}{T} + W3 * \frac{tanh(d(i,j) - d_c)}{T} \right)$$

$$+ \sum_{\substack{|i-j| = 1}} \left(IF_{max} * \frac{tanh(da_{max} - d(i,j))}{T} + W1 * \frac{tanh(d(i,j) - d_{min})}{T} \right)$$

$$tanh: \text{ hyperbolic tangent function}$$

$$IF_{ij}: \text{ interaction frequency between units i and j}$$

$$T: \text{ total interaction frequencies}$$

$$d_c: \text{ contact distance threshold}$$

$$d_{min}: \text{ minimum distance between two units}$$

da_{max}: maximum distance between two adjacent units
 W1, W2, W3, W4: weight parameters in order to
 maximize % satisfied contacts + % satisfied non-contacts

Chromosome	Percentage of contact pairs	W_1	W_2	W_3	W_4
1	49%	2.0	1.0	1.0	1.0
2	55%	2.0	1.0	1.0	1.0
3	66%	1.2	1.0	1.0	1.0
4	65%	1.0	1.0	1.0	1.0
5	64%	1.0	1.1	1.1	1.1
6	70%	1.0	1.2	1.2	1.2
7	74%	1.0	1.5	1.5	1.5
8	77%	1.0	1.6	1.6	1.6
9	75%	1.0	2.2	2.2	2.2
10	78%	1.0	1.8	1.8	1.8
11	77%	1.0	1.8	1.8	1.8
12	75%	1.0	1.5	1.5	1.5
13	94%	1.0	4.6	4.6	4.6
14	86%	1.0	3.5	3.5	3.5
15	89%	1.0	3.0	3.0	3.0
16	86%	1.0	3.9	3.9	3.9
17	85%	1.0	3.0	3.0	3.0
18	97%	1.0	9.5	9.5	9.5
19	92%	1.0	4.0	4.0	4.0
20	93%	1.0	5.0	5.0	5.0
21	94%	1.0	6.0	6.0	6.0
22	96%	1.0	6.0	6.0	6.0
23	83%	1.0	2.0	2.0	2.0

Table S1 The weight parameters and the percent of contacts after removing nose for 23pairs of chromosomes at 1MB resolution.
Estimating Parameters

- FISH data (*Mateos-Langerak et al., 2009*) for physical distances of Chr. 1 and 11 at various genomic distances
- d_{min}, da_{max}: min and max distance between pairs at 1Mb away. (0.2 um , 1.8 um)
- d_{max}: max distance between all pairs
- d_c: a threshold resulting in the same percent of contacts in our data
- d_c and d_{max} are chromosome length dependent (1.73 – 2.24 um, 2.45 – 3.32 um)

Steepest Gradient Ascent with Backtracking Line Search

- **Random Initialization:** $(x_1^0 y_1^0, z_1^0), (x_2^0 y_2^0, z_2^0), ..., (x_N^0 y_N^0, z_N^0)$ in [-0.5, 0.5]
- Update:

$$X_{1}^{t+1} = X_{1}^{t} + \eta^{*} \Delta X \quad Y_{1}^{t+1} = Y_{1}^{t} + \eta^{*} \Delta Y \quad Z_{1}^{t+1} = Z_{1}^{t} + \eta^{*} \Delta Z$$

$$X_2^{t+1} = X_2^t + \eta^* \Delta X$$
 $Y_2^{t+1} = Y_2^t + \eta^* \Delta Y$ $Z_2^{t+1} = Z_2^t + \eta^* \Delta Z$



$$X_N^{t+1} = X_1^t + \eta^* \Delta X \quad Y_N^{t+1} = Y_1^t + \eta^* \Delta Y \quad Z_N^{t+1} = Z_1^t + \eta^* \Delta Z$$

Step size (η) is adjusted dynamically during iterations to avoid too big moves.

Structure Modeling Movie

Structure Modeling Movie

At YouTube without music: <u>http://www.youtube.com/watch?v=C03R7A9kYc8</u>

At NSF CAREER project web site with music: <u>http://people.cs.missouri.edu/~chengji/genome_modeling_movie.mp4</u>

J. Cheng, NSF CAREER Project Plan, 2011, 2012, 2013. T. Tuan made the movie.

Two Compartment Validation on Normal B-Cell





Chromosome 7

Purple and green denote regions in two different components using principle component analysis on contact correlation map

J. Cheng, NSF CAREER Project Plan, 2011, 2012, 2013

Model Selection

- Use TM-Score (Zhang & Skolnick, 2004) to superpose every pair of models in an ensemble of models
- Calculate GDT-HA score: percent of unit pairs within specific distance thresholds
- Choose centroid model as representative

Satisfaction of Contacts in Representative Models of Normal B-Cell

Chromosome	Satisfied contact	Satisfied Non-contact
	pairs (%)	pairs (%)
1	82	80
2	81	80
3	82	84
4	85	85
5	83	86
6	83	83
7	86	82
8	89	83
9	88	90
10	87	88
11	86	86
12	88	88
13	90	89
14	93	84
15	91	90
16	89	88
17	90	92
18	89	94
19	92	96
20	90	90
21	92	99
22	91	92

Violations of Contacts on Normal B-Cell

Chromosome	Average distance	Average IF	Average distance	d _c	Average
	(unsatisfied contact	(unsatisfied contact	(unsatisfied non-contact		IF
	pairs)	pairs)	pairs)		
1	1.98	0.44	1.43	1.73	1.6
2	1.97	0.52	1.48	1.73	1.84
3	1.94	0.60	1.51	1.73	2.09
4	2.05	0.57	1.31	1.73	2.36
5	2.03	0.55	1.39	1.73	2.22
6	1.97	0.60	1.42	1.73	2.23
7	2.37	0.62	1.68	2.00	2.39
8	2.34	0.69	1.60	2.00	2.76
9	2.42	0.72	1.72	2.12	3.49
10	2.58	0.71	1.92	2.23	2.78
11	2.56	0.71	1.80	2.23	2.6
12	2.54	0.67	1.89	2.23	2.69
13	2.55	1.32	1.75	2.23	4.34
14	2.47	1.15	1.69	2.23	4.12
15	2.46	1.02	1.85	2.23	3.78
16	2.58	0.91	1.79	2.34	4.02
17	2.56	0.93	2.06	2.34	3.78
18	2.66	1.36	1.72	2.34	4.54
19	2.57	1.40	1.84	2.34	5.85
20	2.56	1.35	1.78	2.34	4.88
21	2.62	1.60	1.93	2.34	7.28
22	2.58	1.78	1.64	2.34	7.05

3D Models for 22 **Chromosomes** of Normal B-Cell

Chromosome 1 Chromosome 2 Chromosome 5 Chromosome

Chromosome 3









Chromosome 11



Chromosome 20





Chromosome 17







J. Cheng, NSF CAREER Project Plan, 2011, 2012, 2013









Chromosome 19







Models: 200KB resolution

Models of Chr. 2 for Normal and Malignant Cells





Primary Leukemia B-Cell

Normal B-Cell

J. Cheng, NSF CAREER Project Plan, 2011, 2012, 2013



Model Consistency

Trieu T, and Cheng J Nucl. Acids Res. 2014;nar.gkt1411

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The similarity scores measured as average GDT-HA scores. Y-axis denotes the similarity scores and X-axis the indices of chromosomes. 'Blue bars' represent the average GDT-HA scores of models within the same model ensemble constructed from the whole normalized data sets of the normal B-cell for each chromosome, 'red bars' the average GDT-HA scores between models constructed from sampled data sets with those constructed from the whole data sets and 'green bars' the average GDT-HA scores between models of the leukemia B-cell and those of the normal B-cell.

The percentage of recovered contacts in all chromosomes in validation



Trieu T, and Cheng J Nucl. Acids Res. 2014;nar.gkt1411

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Nucleic Acids Research

The superimposition of the plots of IFs of all missing contacts and the plots of IFs of recovered contacts for chromosome 1 (left) and chromosome 11 (right).



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Nucleic Acids Research

Average of spatial distances and IFs of region pairs within and across (between) compartments in chromosomes 1 and 11.



Trieu T, and Cheng J Nucl. Acids Res. 2014;nar.gkt1411

Nucleic Acids Research

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The contact scores and non-contact scores of the chromosomal models of the leukemia Bcell.



Trieu T, and Cheng J Nucl. Acids Res. 2014;nar.gkt1411

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Nucleic Acids Research

The models of chromosome 1 at resolution of 200 K (A) and at resolution of 1 MB (B).



Trieu T, and Cheng J Nucl. Acids Res. 2014;nar.gkt1411

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Nucleic Acids Research



Pairwise comparison:

1Mb versus 200Kb

$$\begin{aligned} & \text{Scoring Function for Genome} \\ & \text{Optimization} \\ Fn = \sum_{\{(i,j): |i-j|\neq 1\}} \left(W_1[chr1, chr2] * tanh(d_c^2 - d_{ij}^2) * \frac{F_{ij}}{totallF} + \\ & W_2[chr1, chr2] * \frac{tanh(d_{ij}^2 - d_{min}^2)}{totallF} \right) + \\ & \sum_{\{(i,j): |i-j|=1 & chr1=chr2\}} \left(W_1[chr1, chr2] * IF_{max} * \frac{tanh(da_{max}^2 - d_{ij}^2)}{totallF} + \\ & \text{Adjacent Pairs} \\ & W_2[chr1, chr2] * \frac{tanh(d_{ij}^2 - d_{min}^2)}{totallF} \right) + \\ & \sum_{\{(i,j): |i-j|\neq 1, chr1=chr2\}} \left(W_3[chr1, chr1] * \frac{tanh(d_{max,intra}^2 - d_{ij}^2)}{totallF} + \\ & W_4[chr1, chr1] * \frac{tanh(d_{ij}^2 - d_{min}^2)}{totallF} \right) + \\ & \sum_{\{(i,j): |i-j|\neq 1, chr1=chr2\}} \left(W_3[chr1, chr2] * \frac{tanh(d_{max,inter}^2 - d_{ij}^2)}{totallF} + \\ & W_4[chr1, chr1] * \frac{tanh(d_{ij}^2 - d_{min}^2)}{totallF} \right) + \\ & \sum_{\{(i,j): |i-j|\neq 1, chr1\neq chr2\}} \left(W_3[chr1, chr2] * \frac{tanh(d_{max,inter}^2 - d_{ij}^2)}{totallF} + \\ & W_4[chr1, chr2] * \frac{tanh(d_{ij}^2 - d_{min}^2)}{totallF} \right) \end{aligned}$$

 $d_{min}^2 = 0.2 \ \mu m^2, \ da_{max}^2 = 1.8(\mu m^2)$ $d_c^2 = 6\mu m^2, \ d_{max_intra}^2 = d_{max}^2 = 20\mu m^2$ $d_{max_inter} = 13\mu m$

Modeling of 3D Genome



Test on Simulated Data of the Yeast Genome Structure



Known Structure (Duan et al., 2010)





A 3D Model of Genome of Human B-Cell in an Ensemble



Largely Conserved Chromosomal Structure, Dynamic Genome Structure



Chromosome 11

Pairwise structural similarity between chromosomal models: 0.71 Pairwise structural similarity between genome models: 0.16

Center – Periphery Architecture and Dynamic Inter-chromosomal Interactions



- Small chromosomes in center
- Large chromosomes in periphery
- Genome structure ensemble (dynamics)
- Correlation of inter-chromosomal interactions

 (0.48), p-value < e-16
 Trieu, Cheng, Bioinformatics, 2016

Enriched Telomere and Centromere Inter-Chromosomal Interactions



 Telomere-telomere interactions > telomere/centromere interactions > other interactions

MOGEN: Model of Genome (Tool)



- 2. <u>Genome structures of healthy cells: http://calla.rnet.missouri.edu/mogen/normal_cell/</u>
- 3. <u>Genome structures of malignant cells: http://calla.rnet.missouri.edu/mogen/cancer_cell/</u>
- 4. <u>Experimental data on synthetic datasets:</u> <u>https://missouri.box.com/s/5cnwys9e1qgt8o20pdh8544meb5myay0</u>
- 5. MOGEN: Executable program https://missouri.box.com/s/a8nynitxow4aixj6fd0k2xf6n4wof772

http://calla.rnet.missouri.edu/mogen/

MOGEN at GitHub

- <u>https://github.com/BDM-Lab/MOGEN</u>
- Trieu, Tuan, and Jianlin Cheng. "MOGEN: a tool for reconstructing 3D models of genomes from chromosomal conformation capturing data." *Bioinformatics* 32.9 (2015): 1286-1292.

Secure https://github.com/BDM-Lab/MOGEN

The software for modeling the 3D structure of a genome using Hi-C chromosome conformation capturing data

🕝 19 commits	ဖို 1 branch	🛇 1 release	a contributor	å_ GPL-3.0
Branch: master - New p	ull request		Fin	d file Clone or download -
💽 tuan add buildfile			Latest com	nmit 07e31c6 on Mar 10, 2017
🖬 bin	MOGEN sour	ce code		2 years ago
documents	add supplem	entary document		a year ago
examples/hiC	remove file >	100 mb		2 years ago
src	add supplem	entary document		a year ago
	Initial commi	t		2 years ago
README.md	add question	3		a year ago
build.xml	add buildfile			a year ago
E README.md				
			_	
MOGEN: The chromosom	e software for mode e conformation cap	ling the 3D structu turing data	re of a genome using	Hi-C

3D Structure of the Entire Genome



Smaller Chromosomes are Closer to the Center







GMOL - Multi-Scale Visualization of 3D Genome Structure



Project 4

- Apply a gradient descent method LorDG / MOGEN to build 3D models for human chromosome 7.
- References: (1) T. Trieu, J. Cheng. 3D Genome Structure Modeling by Lorentzian Objective Function. Nucleic Acids Research, accepted, 2016; (2) Trieu, Cheng. Large-scale reconstruction of 3D structures of human chromosomes from chromosomal contact data. Nucleic Acids Research, 2014; (3) T. Tuan, J. Cheng. MOGEN: a tool for reconstructing 3D models of genomes from chromosomal conformation capturing data. Bioinformatics, accepted, doi: 10.1093/bioinformatics/btv754.
- How to assess the models (check the paper)?
- Visualization of models
- Reference models (constructed from somewhat different contact data of Chr. 7: <u>http://calla.rnet.missouri.edu/mogen/</u>
- LorDG at GitHub: <u>https://github.com/BDM-Lab/LorDG</u>
- MOGEN at GitHub: <u>https://github.com/BDM-Lab/MOGEN</u>

Data II: Hi-C data of Chromosome 7

HWI-EAS313_0025:7:78:7863:19096|7 40786044 7 45502707|case 0 HWI-EAS313_0025:7:63:14188:6924|7 128562332 7 128562745|case 0 HWI-EAS313_0025:7:94:3739:17610|7 154672365 7 154672125|case 0 HWI-EAS313_0025:7:78:17921:8167|7 90166635 7 90166267|case 0 HWI-EAS313_0025:7:98:5753:2860|7 146851262 7 82792917|case 0 WI-EAS313_0025:7:104:3993:13804|7 101472788 7 101472557|case 0 HWI-EAS313_0025:7:4:13123:19420|7 63615352 7 62522230|case 0 HWI-EAS313_0025:7:54:7610:3364|7 24688078 7 24687498|case 0 HWI-EAS313_0025:7:6:8245:1169|7 47788402 7 47788122|case 0

http://sysbio.rnet.missouri.edu/3dgenome/contact ALL chrom7

The LorDG /MOGEN software package includes some sample data and examples of how to run the program.

Timeline

- April 30: discussion of plan
- May2: presentation of the plan
- May 9: Presentation of your results

Acknowledgements

- Tuan Trieu, Oluwatosin Oluwadare, Chenfeng He, Sharif Ahmed, Lingfei Xu
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